

Condensation and pattern formation in cold exciton gases

L.V. Butov^{1,2}, L.S. Levitov³, A.V. Mintsev^{1,2}, B.D. Simons⁴, A.L. Ivanov⁵,
A. Imamoglu⁶, P.B. Littlewood⁴, Y.E. Lozovik⁷, A.A. Shashkin¹,
V.T. Dolgoplov¹, K.L. Campman⁶, A.C. Gossard⁶, D.S. Chemla^{2,8}

¹ *Institute of Solid State Physics RAS, Chernogolovka*

² *E.O. Lawrence Berkeley National Laboratory*

³ *MIT*

⁴ *Cavendish Laboratory, Cambridge*

⁵ *Cardiff University*

⁶ *University of California at Santa Barbara*

⁷ *Institute of Spectroscopy RAS, Troitsk*

⁸ *University of California at Berkeley*

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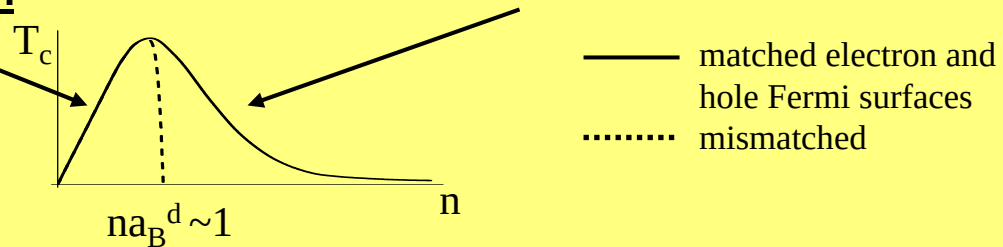
exciton condensation

dilute exciton gas ($na_B^d \ll 1$)

excitons are weakly interacting Bose particles
exciton condensation is analogous to
Bose-Einstein condensation

dense electron-hole system ($na_B^d \gg 1$)

excitons are formed at Fermi level like Cooper pairs
exciton condensate called excitonic insulator
is analogous to BCS superconductor state



L.V. Keldysh, Yu.E. Kopaev (1964)

L.V. Keldysh, A.N. Kozlov (1968)

why it's interesting?

- exciton condensate is a new form of matter
- high T_c for exciton BEC due to light exciton mass: $T_c^{\text{exciton}} \sim 1 \text{ K} \rightarrow$
- possibility to study crossover from BEC to BCS-like state
- possibility of manipulating condensate in microscopic semiconductor devices

Kelvin for excitons



microKelvin for atoms

how to get cold exciton gas?

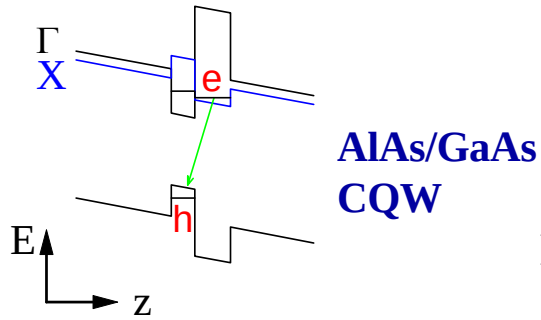
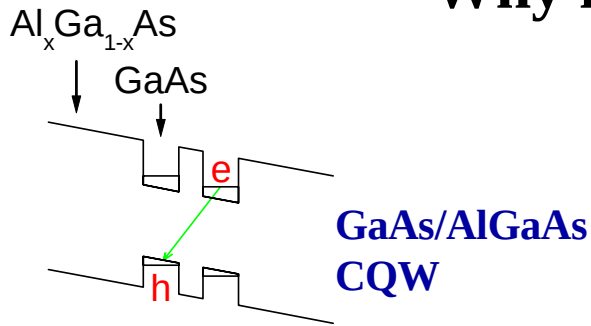
$T_{\text{lattice}} \ll 1 \text{ K}$ in He refrigerators

finite lifetime of excitons could result to high exciton temperature: $T_x > T_{\text{lattice}}$

T_x is determined by the ratio of the exciton lifetime and cooling time

lifetime $\gg$ cooling time $\Rightarrow T_x \sim T_{\text{lattice}}$

Why indirect excitons in CQWs?

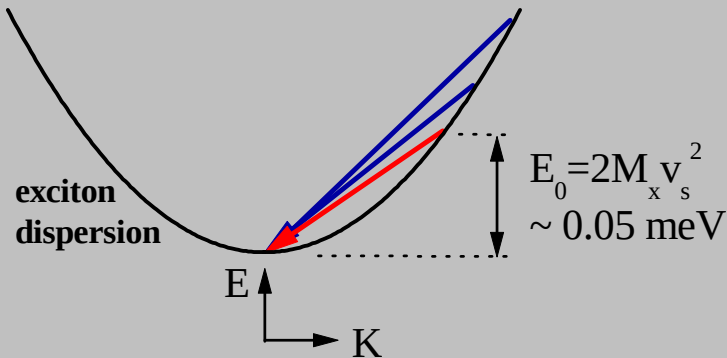


long exciton lifetime due to separation
between electron and hole layers
 10^3 times shorter exciton cooling time
than that in bulk semiconductors

coldest exciton gas: $T_x \ll 1\text{K} < T_c$

potential candidate for realization of exciton condensation

exciton energy relaxation
by LA-phonon emission



3D: coupling of $E=0$ state to single state $E=E_0$
2D: coupling of $E=0$ state to continuum of energy states $E > E_0$

effective cooling of 2D excitons by bulk phonons

How to get cold exciton gas?

excitons are generated hot and cool down to T_{lattice} via phonon emission

T_X drops down
to 400 mK in 5 ns
↑ ↑
 $< T_c$ $\ll$ lifetime

ways to overcome the obstacle of hot generation and study cold gases of indirect excitons with $T_X \sim T_{\text{lattice}}$

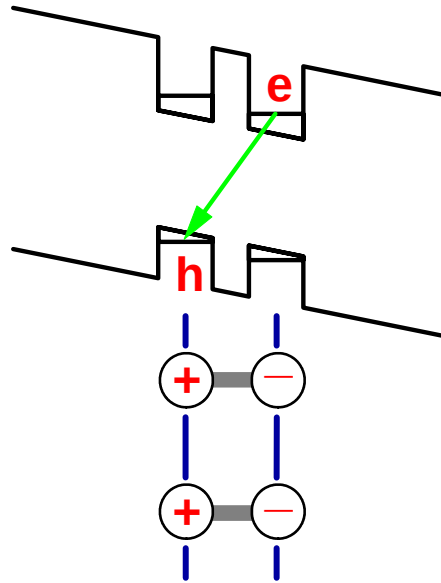
discrimination in time

study indirect excitons
a few ns after the end of
photoexcitation pulse

discrimination in space

study indirect excitons
excitons beyond
photoexcitation spot

Repulsive interaction between indirect excitons



indirect excitons are oriented dipoles

dipole-dipole repulsive interaction

stabilizes exciton state against formation of metallic electron-hole droplets

D. Yoshioka, A.H. MacDonald, J. Phys. Soc. Jpn. 59, 4211 (1990)

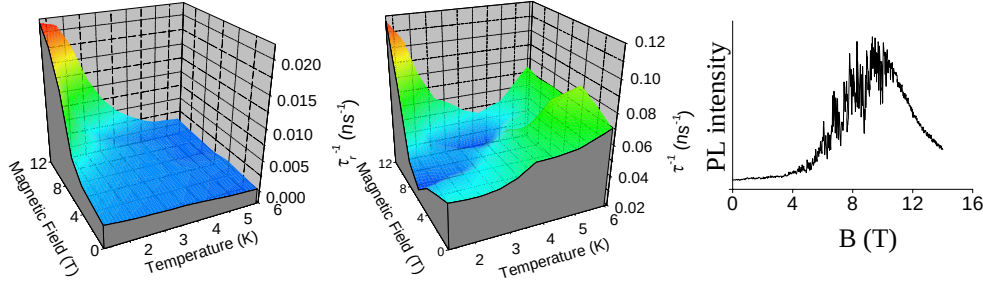
X. Zhu, P.B. Littlewood, M. Hybertsen, T. Rice, PRL 74, 1633 (1995)

results in effective screening of in-plane disorder

A.L. Ivanov, EPL (2002)

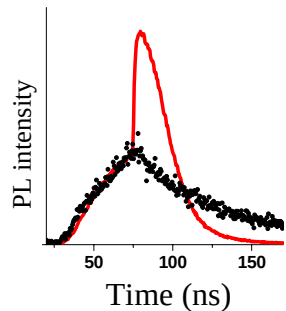
the ground state
of the system
is excitonic

Experiments on exciton condensation in CQW nanostructures



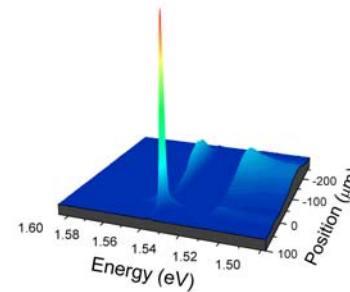
effects indicating exciton condensate superradiance (macroscopic dipole), onset of exciton superfluidity, and fluctuations near phase transition

Butov et al. *J. de Physique* 3, 167 (1993)
PRL 73, 304 (1994)
PRB 58, 1980 (1998)



bosonic stimulation of exciton scattering - signature of degenerate Bose-gas of excitons

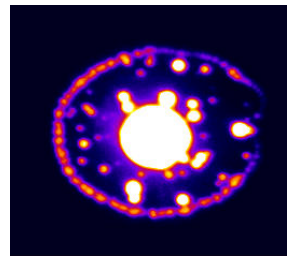
Butov et al. PRL 86, 5608 (2001)
PRL 87, 216804 (2001)



shrinkage of spatially localized exciton cloud with reducing T → degenerate exciton gas

Butov et al. *Nature* 417, 47 (2002)

difference between quasi-condensate – macroscopic occupation of low energy states and BEC – macroscopic occupation of ground state – is not essential for most experiments [V.N. Popov (1972)] and unambiguous distinguishing between them in experiments is hard (if possible)

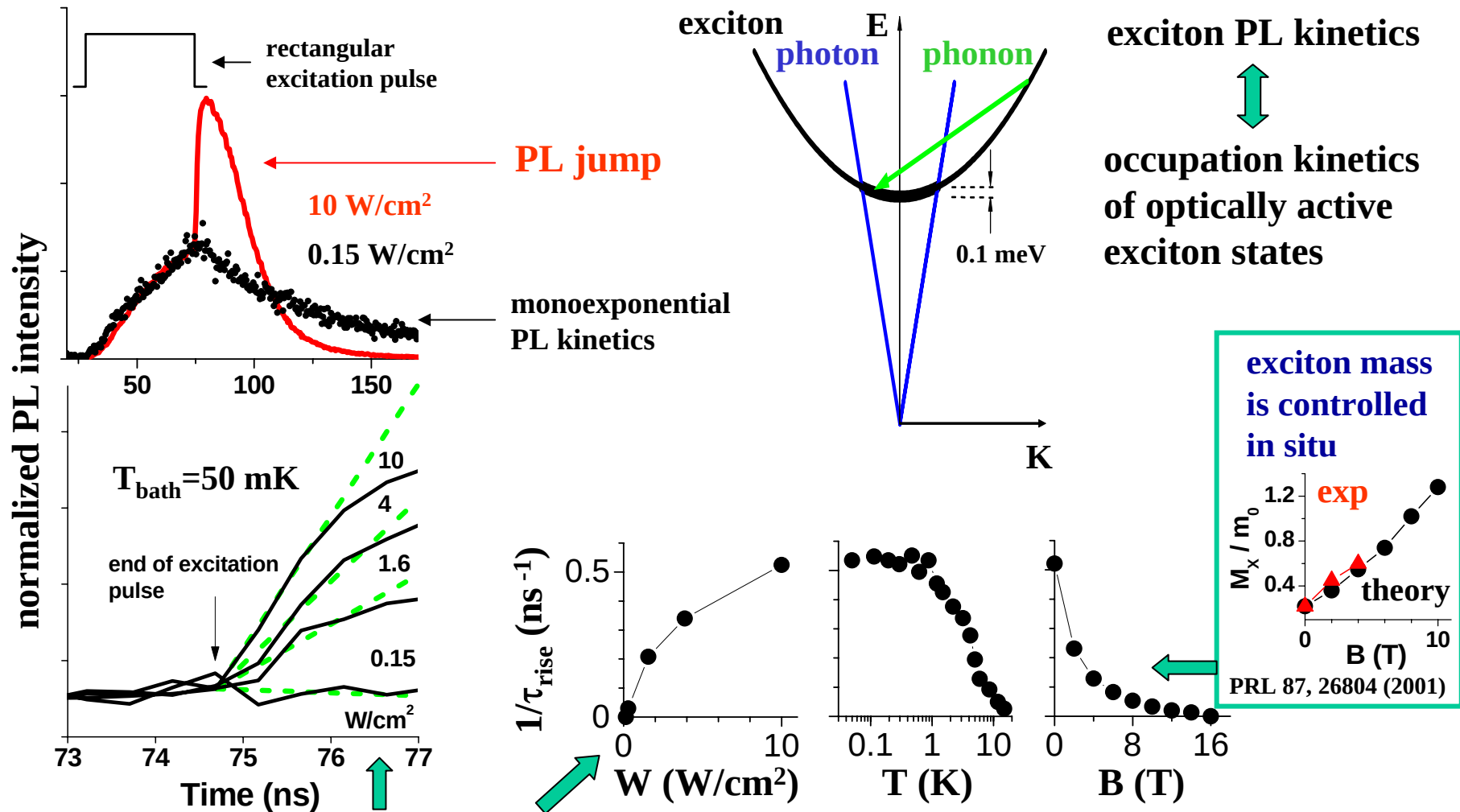


macroscopically ordered exciton state

Butov et al. *Nature*, 418, 751 (2002)

<http://www.lbl.gov/~butov/>
<http://www.issp.ac.ru/butov/>

Bosonic stimulation of exciton scattering

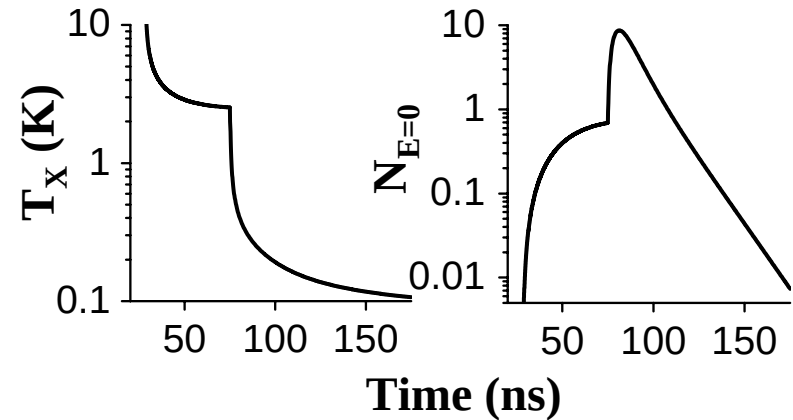
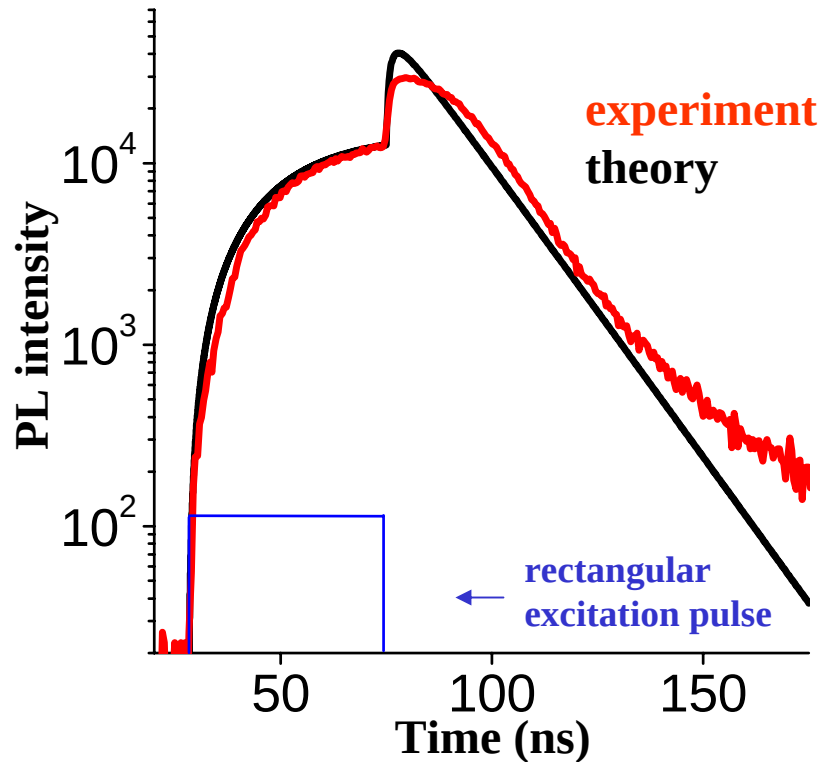


enhancement of exciton scattering rate to low energy states with increasing exciton concentration reveals bosonic stimulation of exciton scattering

signature of degenerate Bose-gas of excitons

scattering rate of bosons to a state p is $\sim(1+N_p)$

Experiment vs theory



$$N_{E=0} = e^{T_0/T_x} - 1$$

$$T_0 = \pi \hbar^2 n / 2 M_X k_B$$

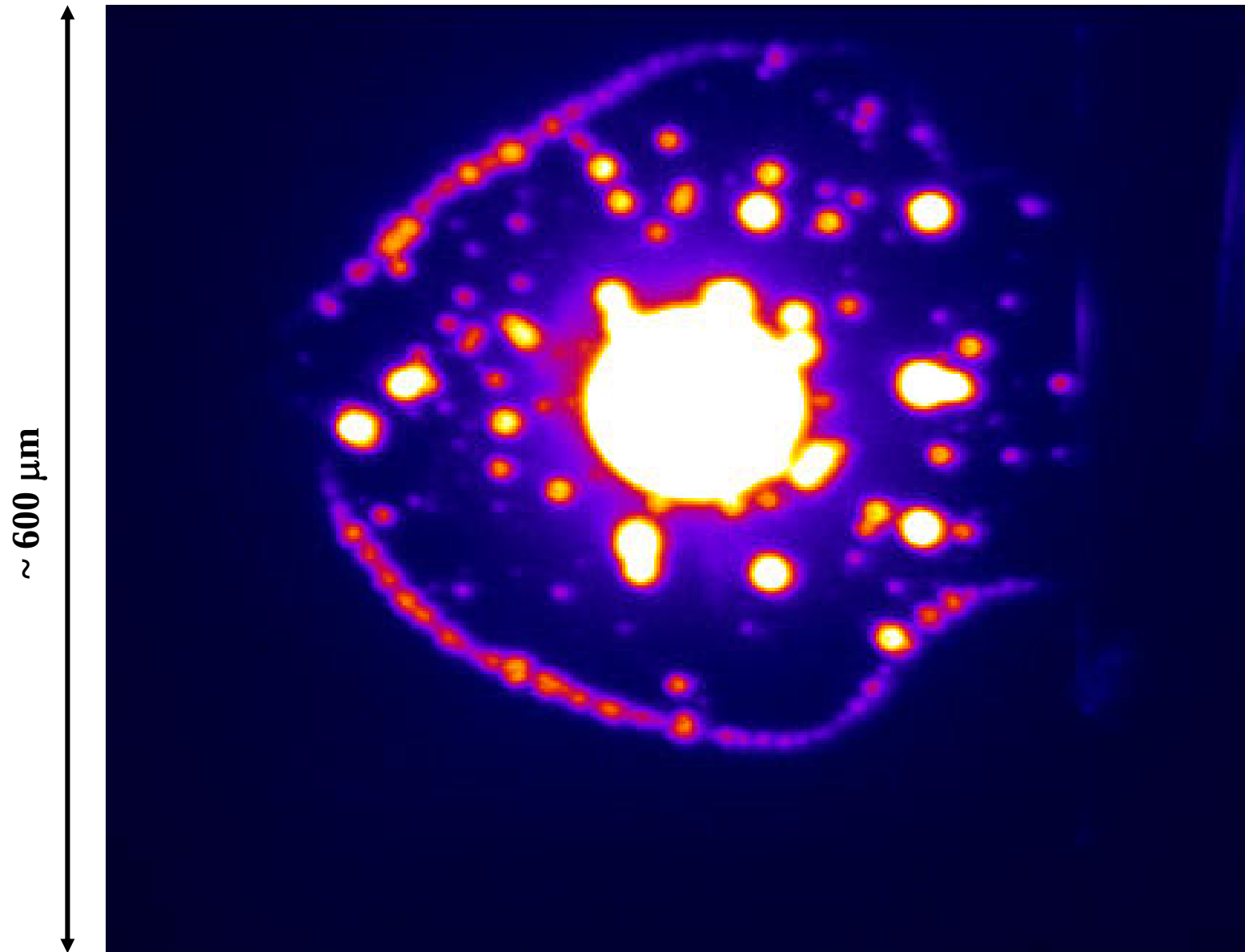
temperature of quantum degeneracy

$$\begin{aligned} dN_{E=0}/dt &= \Gamma_{ph} N_E (1 + N_{E=0}) (1 + n_E^{ph}) - \Gamma_{ph} (1 + N_E) N_{E=0} n_E^{ph} - N_{E=0} / \tau = \\ &= \Gamma_{ph} (N_E - n_E^{ph}) N_{E=0} + \Gamma_{ph} (1 + n_E^{ph}) N_E - N_{E=0} / \tau \end{aligned}$$

at low $T_{lattice}$ and in presence
of generation of hot excitons
 $N_E - n_E^{ph} > 0$

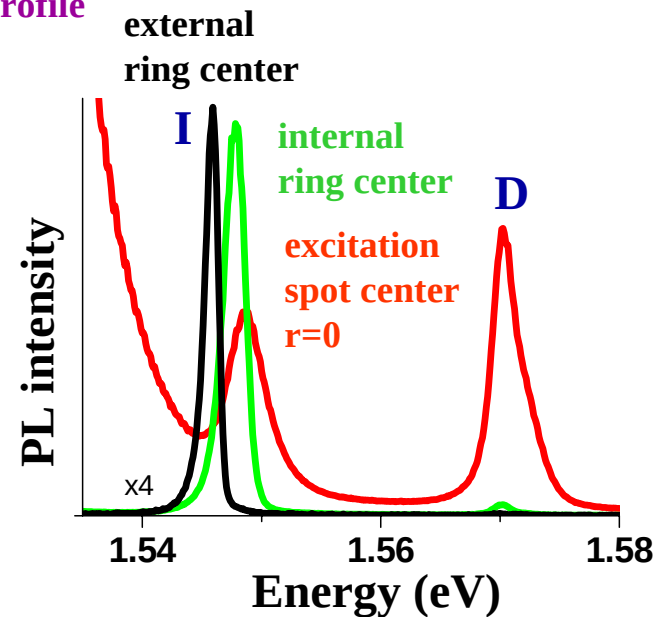
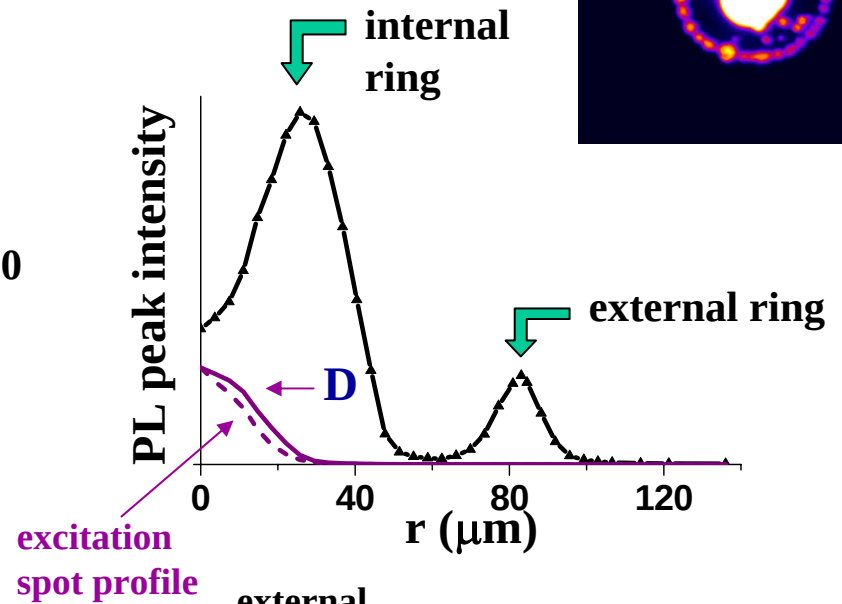
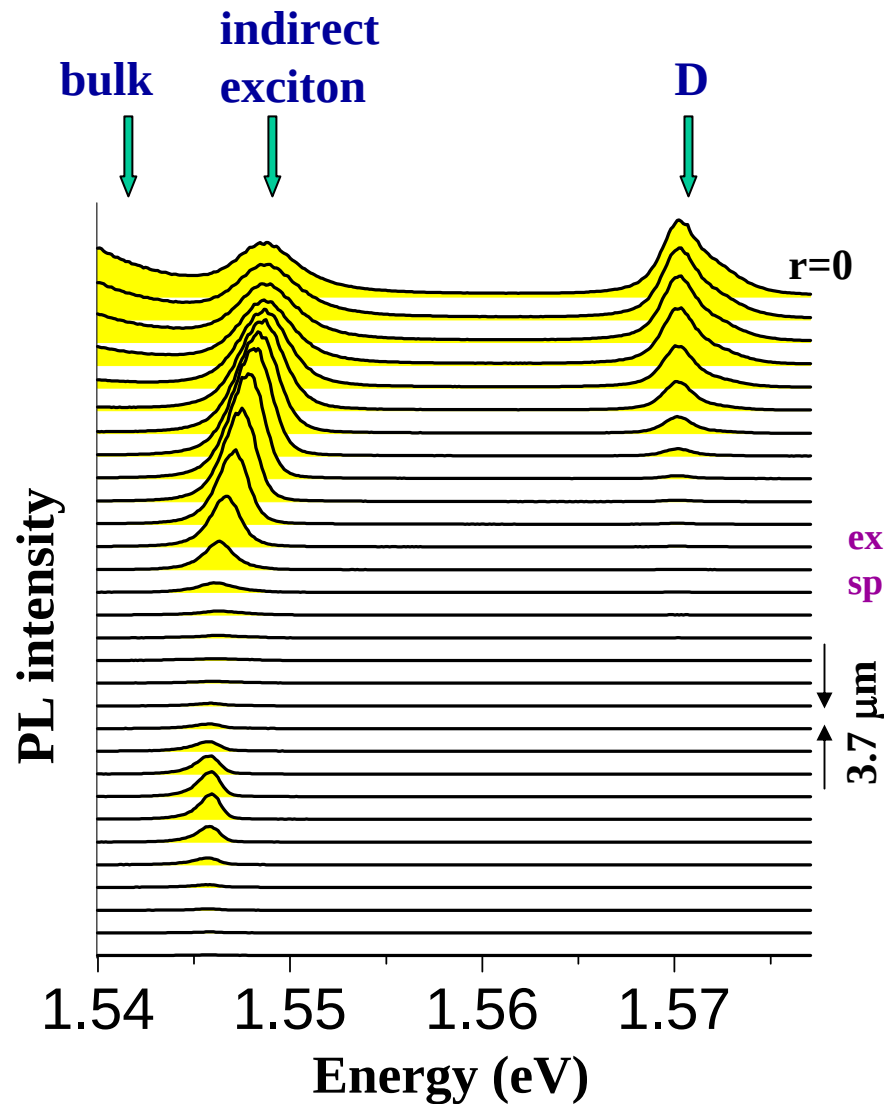
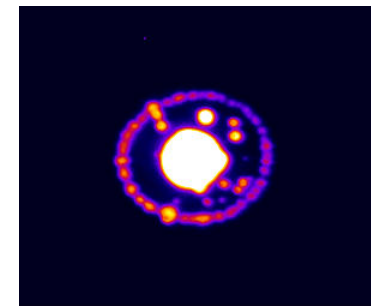
Frolich inversion condition
counterpart of population
inversion condition for lasers

2D image of indirect exciton PL vs P_{ex}

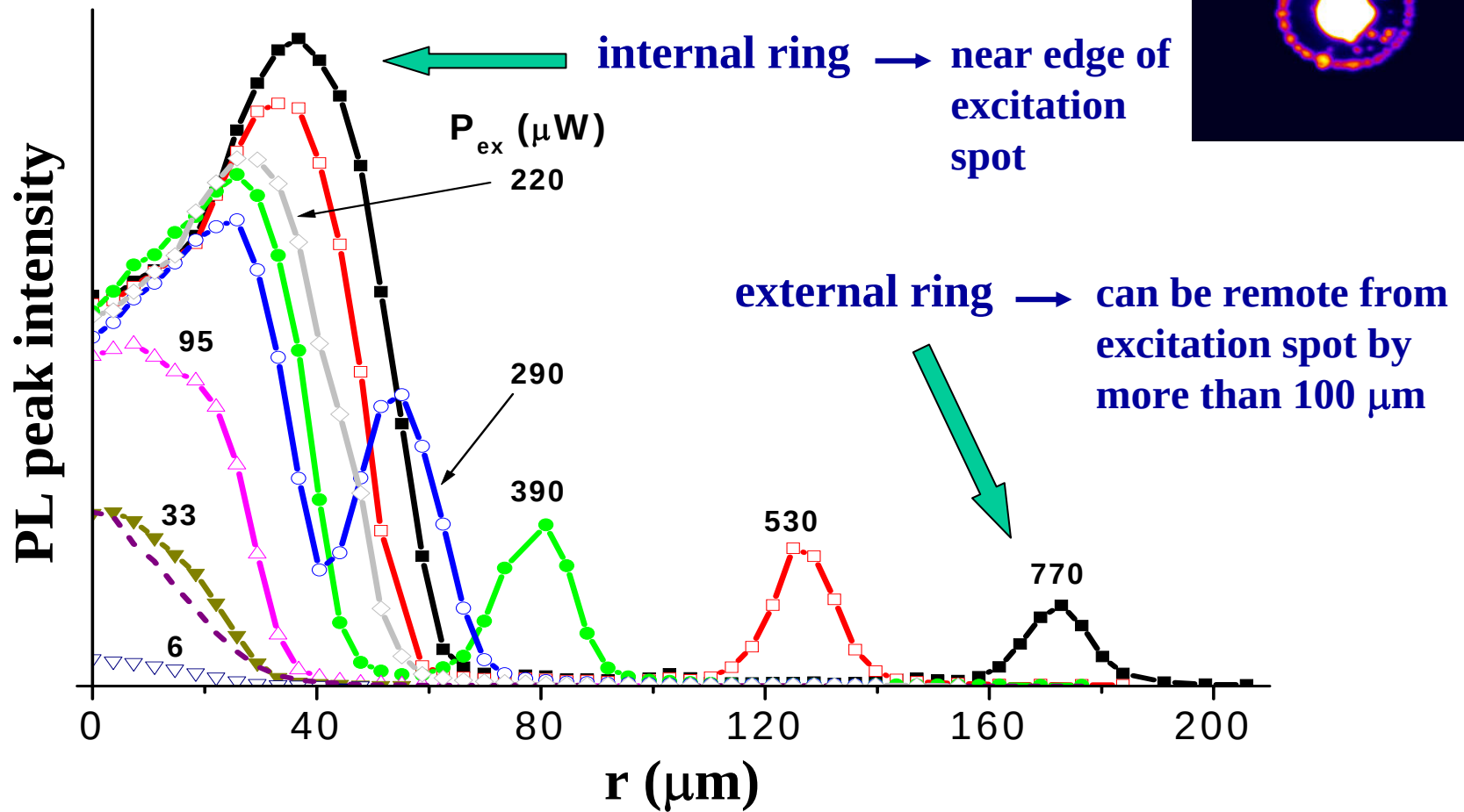
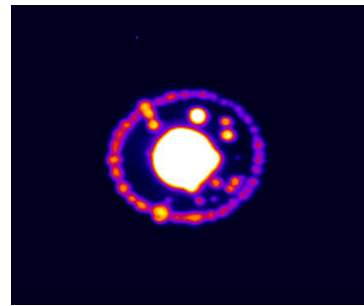


L.V. Butov, A.C. Gossard, and D.S. Chemla, cond-mat/0204482 [Nature 418, 751 (2002)]

Radial dependence of indirect exciton PL



Ring structure of indirect exciton PL



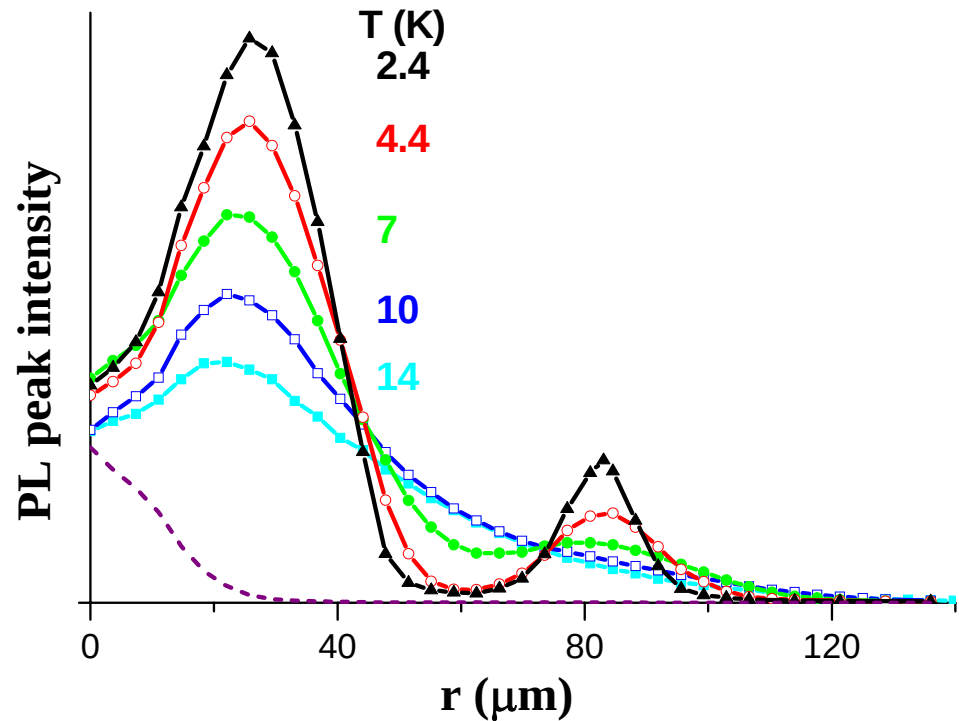
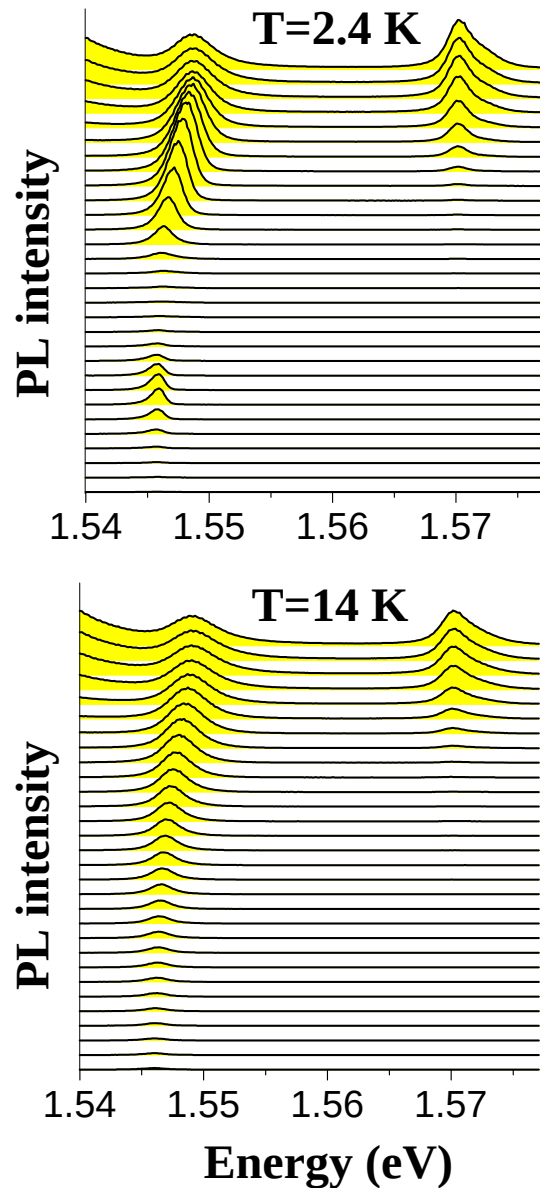
at low densities:

spatial profile of indirect exciton PL intensity follows laser excitation intensity

at high densities:

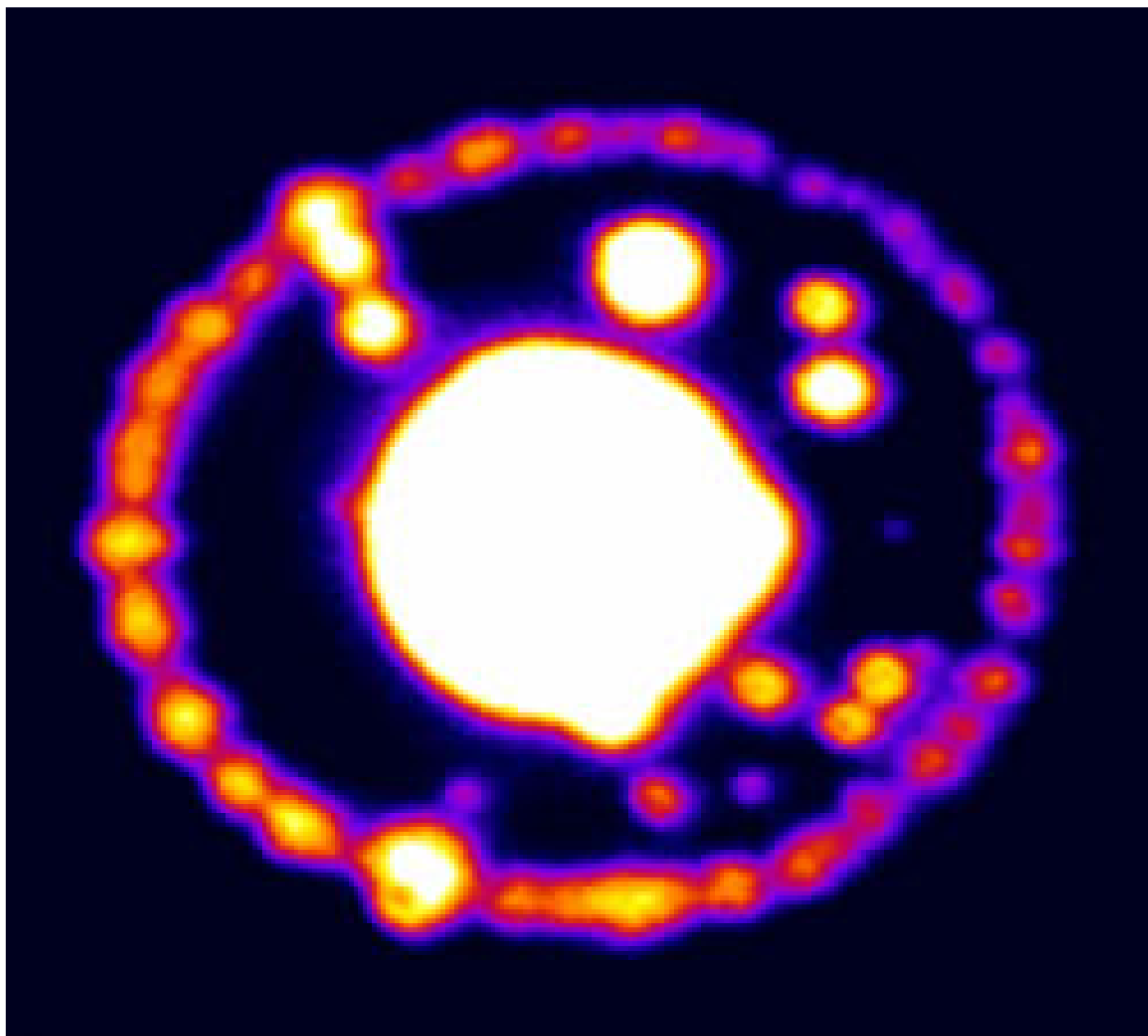
spatial profile of indirect exciton PL intensity is nontrivial $\leftarrow$ ring structure

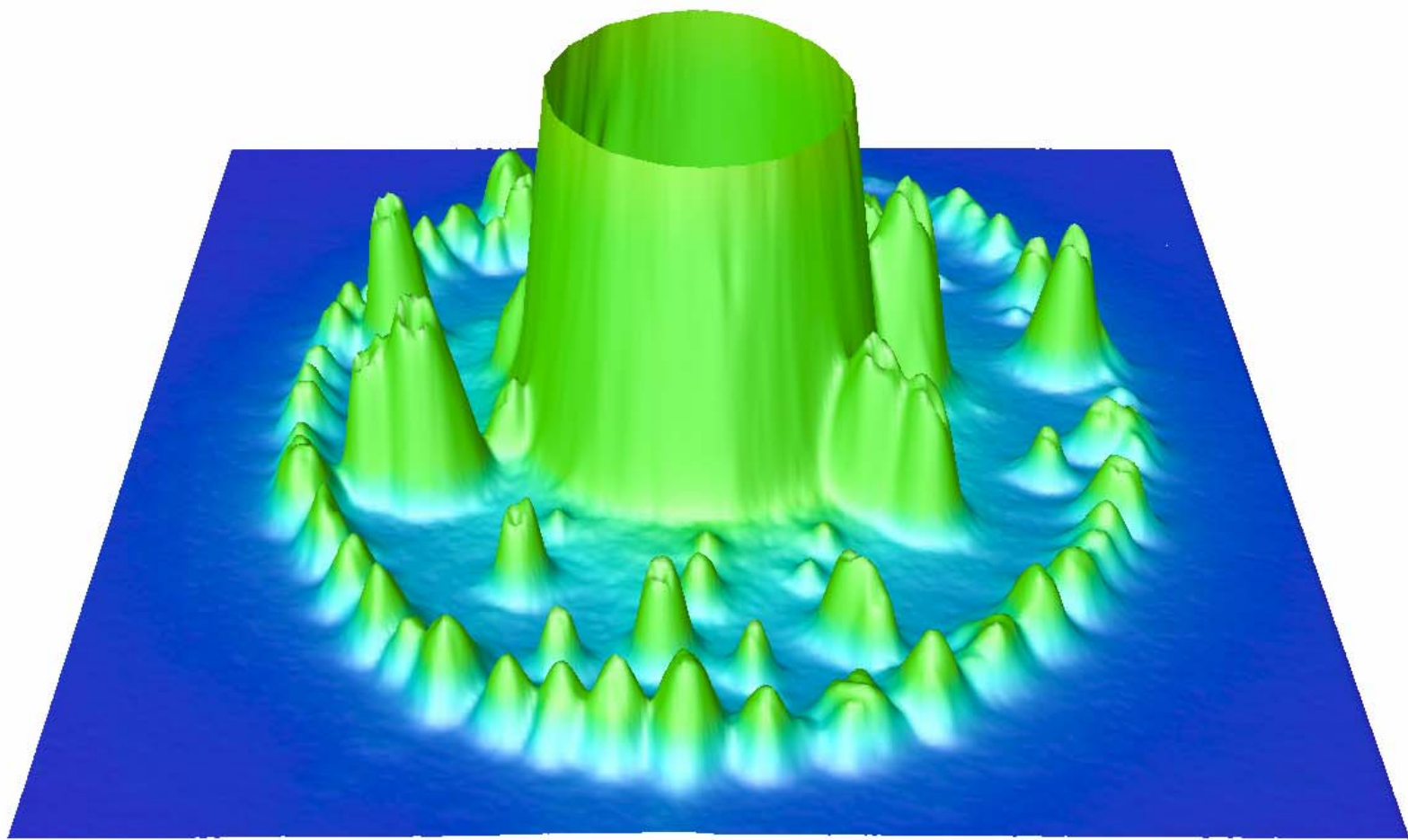
Temperature dependence of ring-shaped PL structure

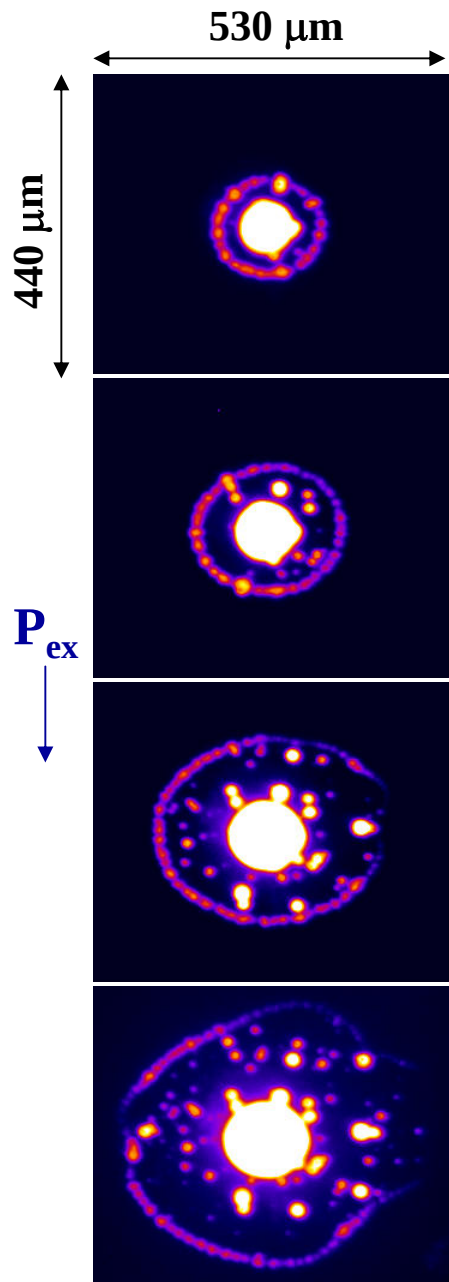


**nontrivial spatial profile of indirect exciton
PL intensity is observed at low T only**

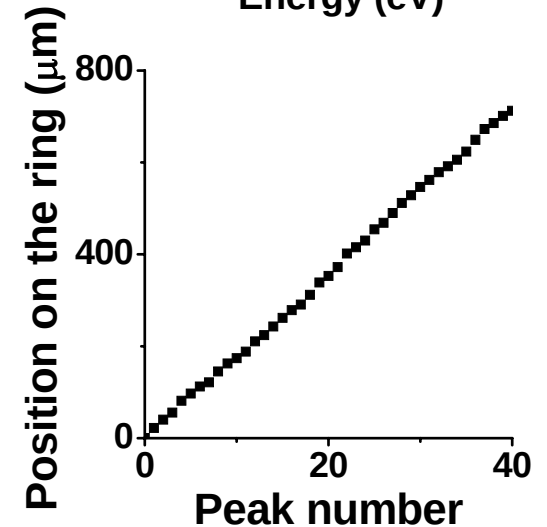
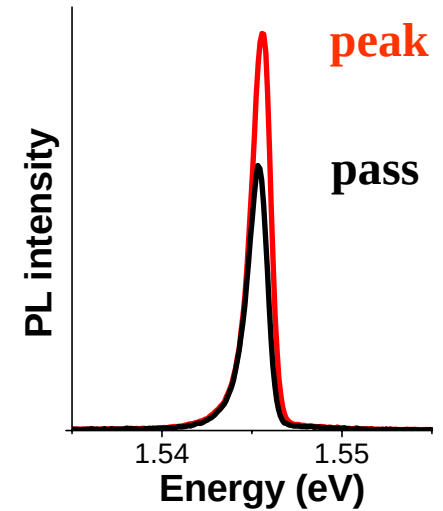
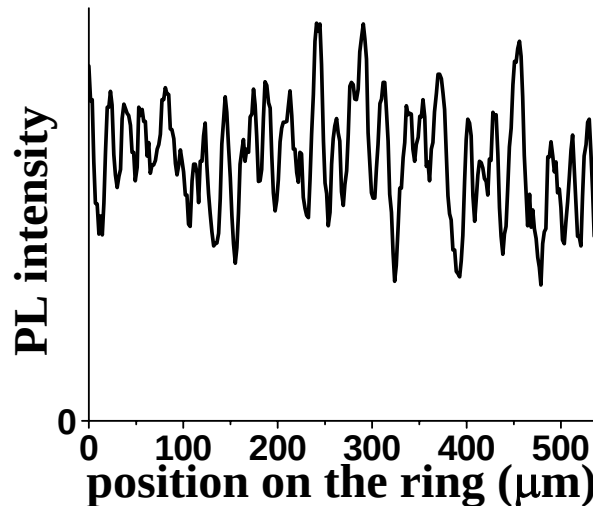
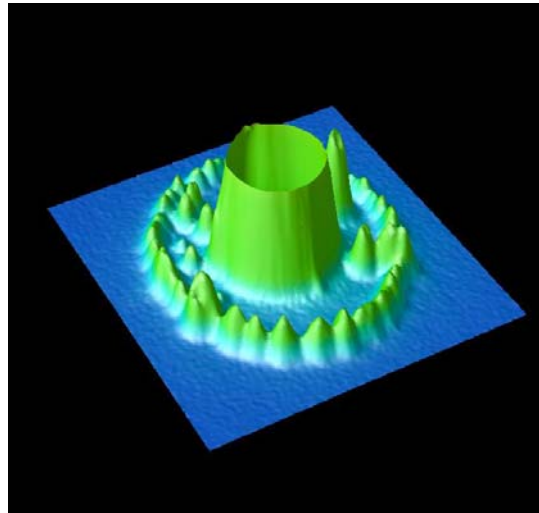
**with increasing T rings wash out and spatial
profile approaches monotonic bell-like shape**





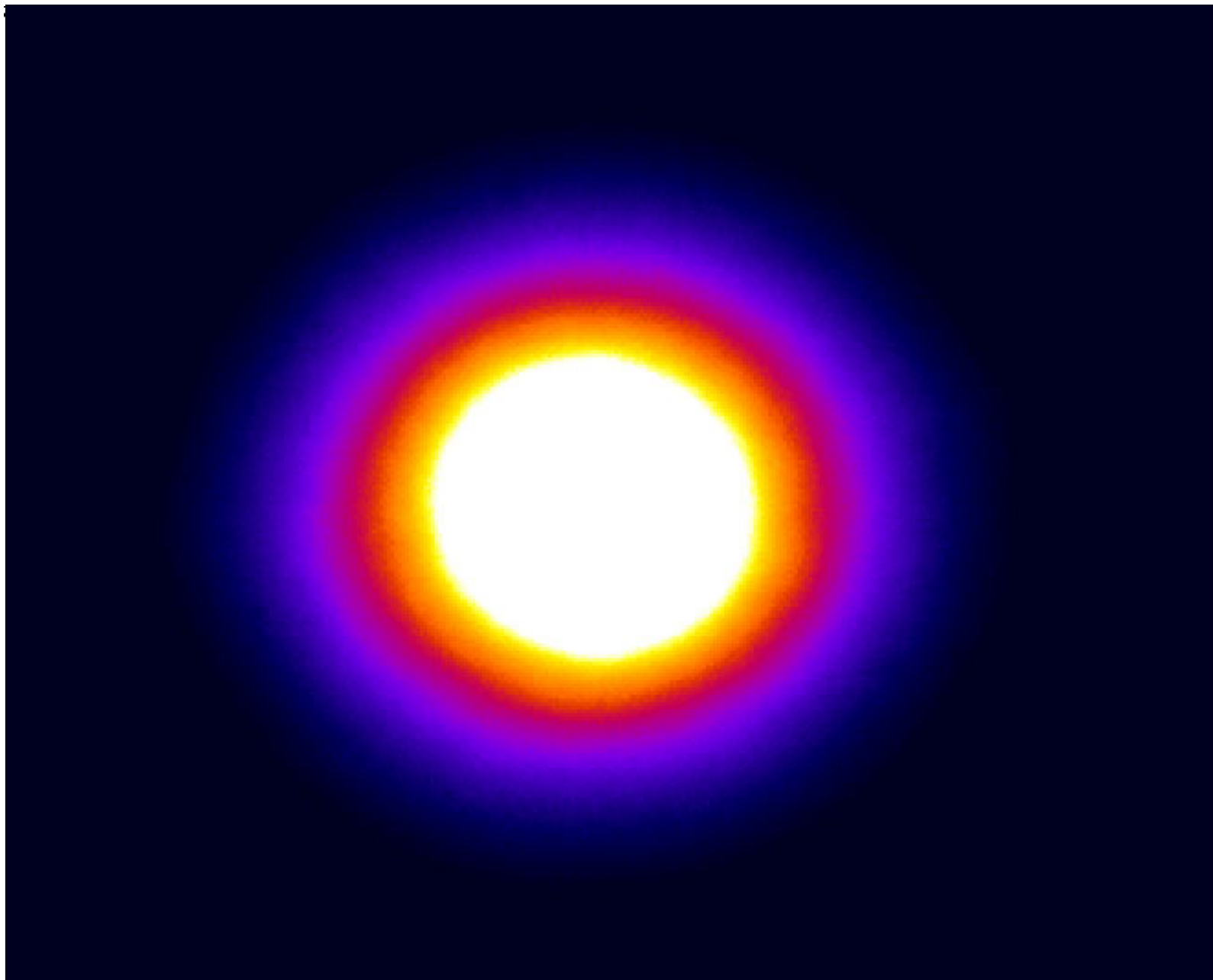


Ring fragmentation



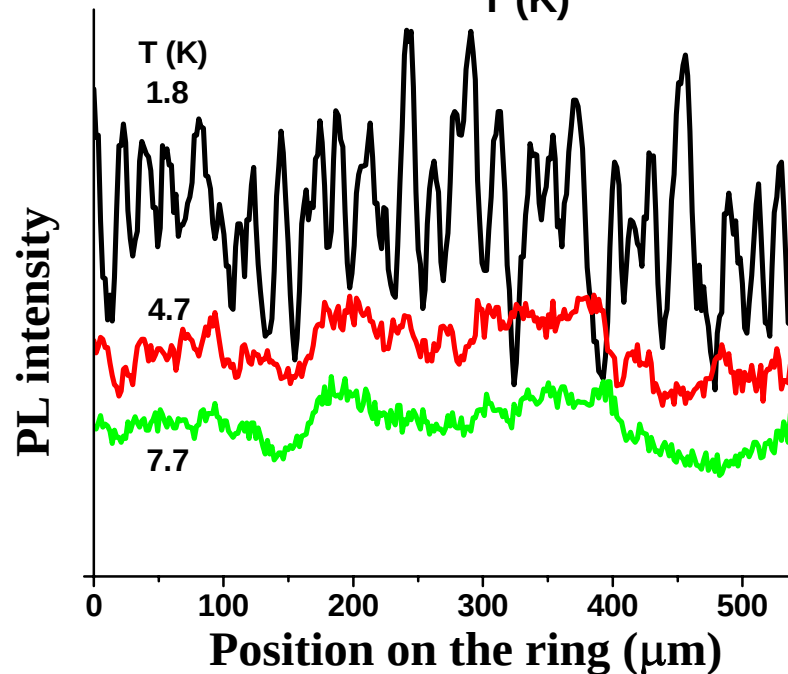
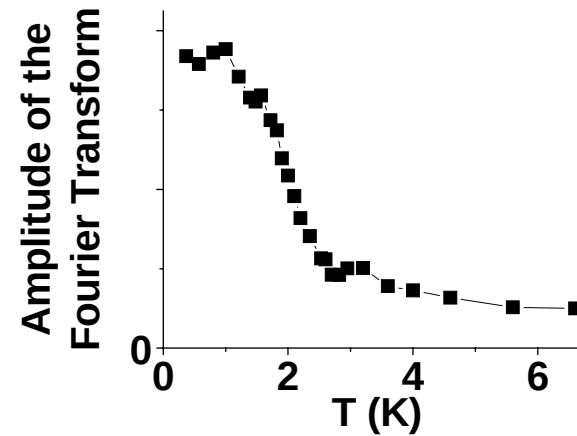
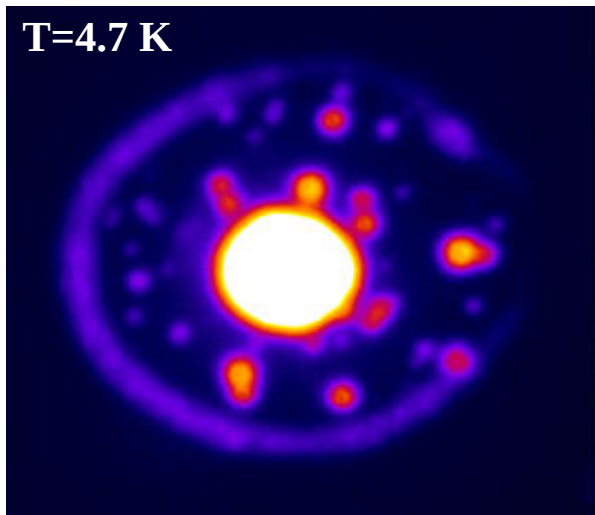
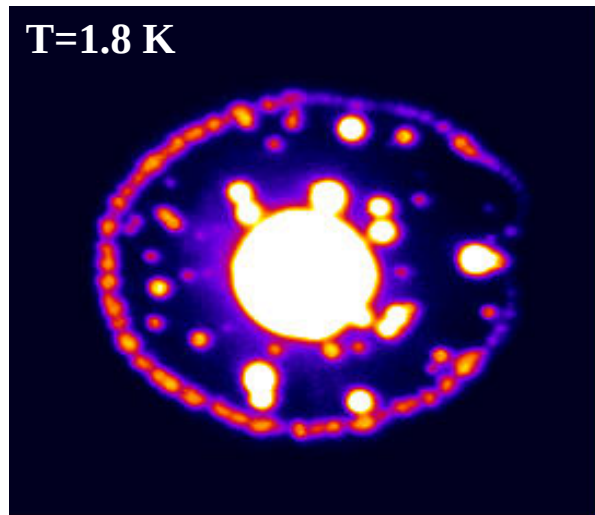
external ring is fragmented into circular-shaped structures that form periodic array over macroscopic lengths, up to ~ 1 mm

2D image of indirect exciton PL vs temperature



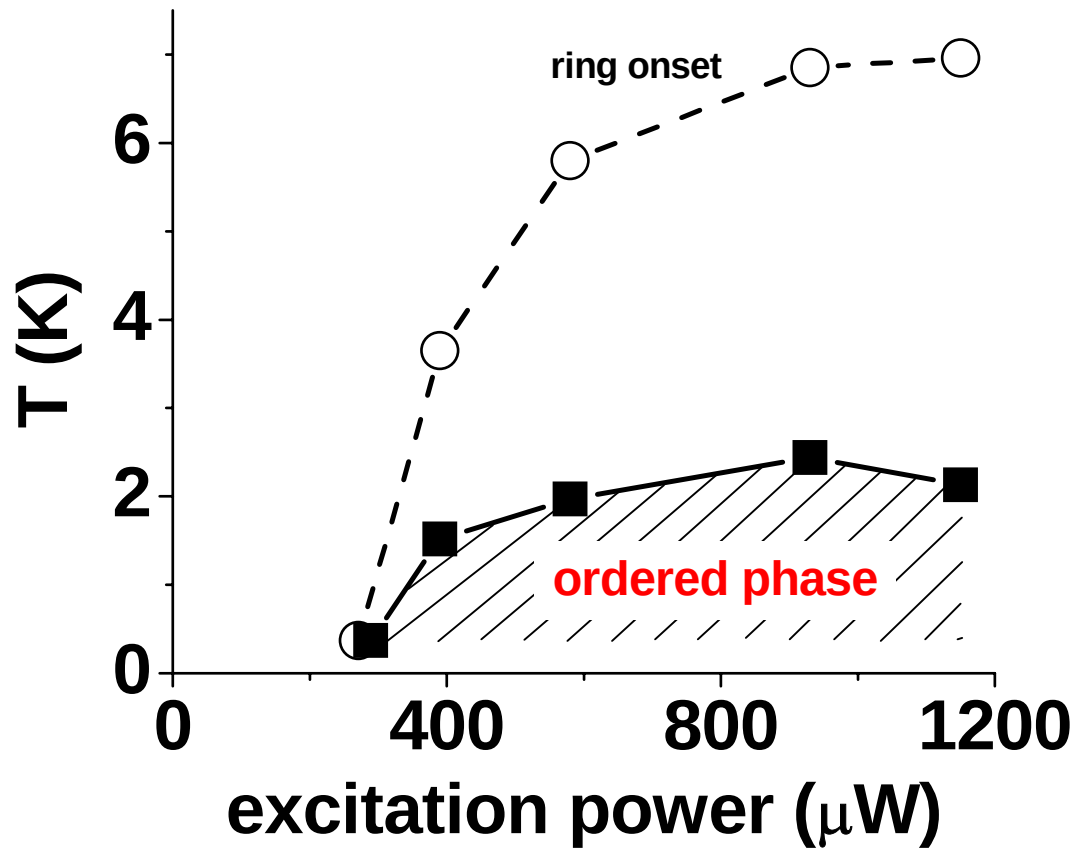
T=0.38-20 K

Temperature dependence of ring fragmentation into spatially ordered array of beads



ring fragmentation into spatially ordered array of beads appears abruptly at low T

Ordered phase



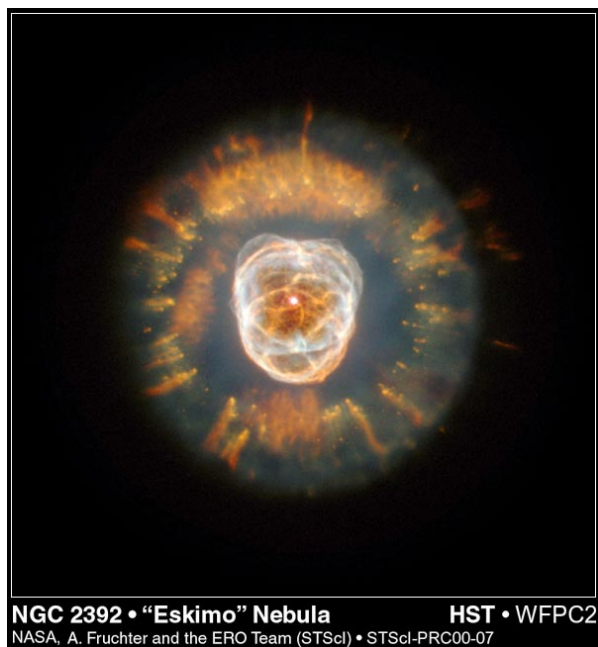
Discussion

origin of the rings

on origin of the macroscopically ordered exciton phase

L.V. Butov, L.S. Levitov, A.V. Mintsev, B.D. Simons, A.C. Gossard, D.S. Chemla, unpublished

Similarities in astrophysics: ring structure of expanding matter

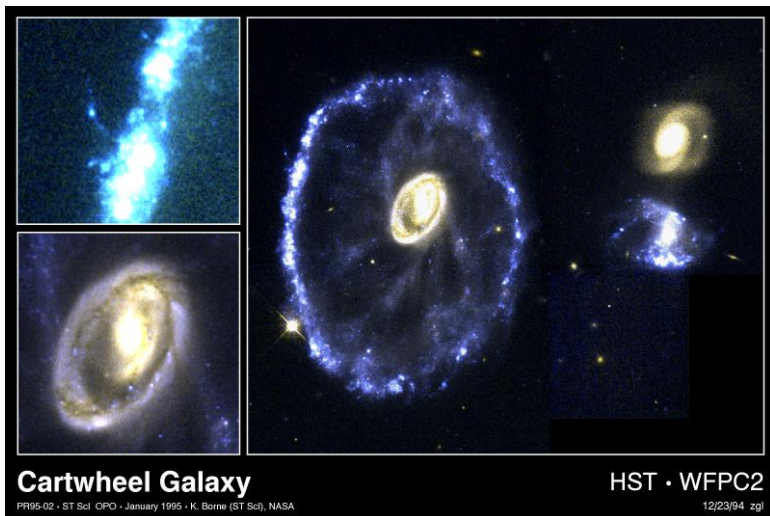


ring structures are generic for systems with centrally symmetric mass flow

a planetary nebula - represents the final stage in the evolution of a Sun-like star

the nebular shells with textures are formed by the wind of material ejected by the star

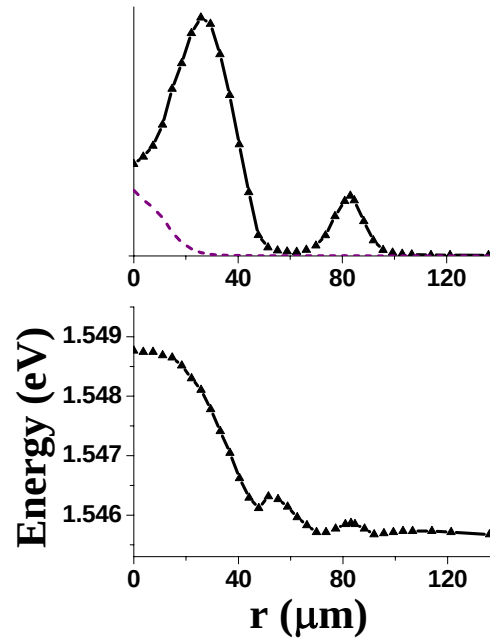
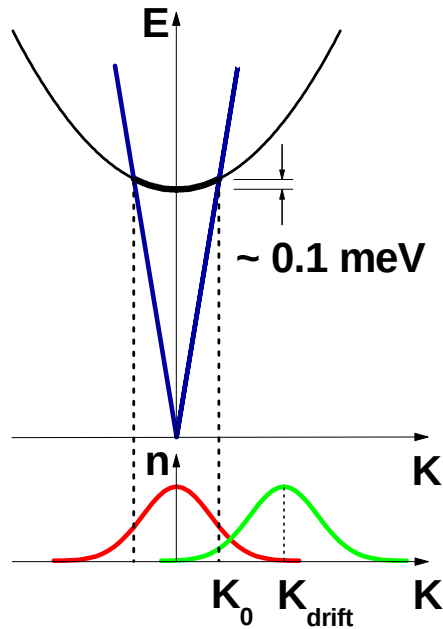
↑
Rayleigh-Taylor instability ?



“...head-on collision between two galaxies.”
“Like a rock tossed into a lake, the collision sent a ripple of energy into space, plowing gas and dust in front of it ... this cosmic tsunami leaves in its wake a firestorm of new star creation ... in large fragmented gas clouds.”

from <http://hubblesite.org>

PL pattern $\longleftrightarrow$ spatial distribution of optically active low energy excitons



continuous flow of excitons
out of excitation spot due to
exciton drift, diffusion, phonon
wind, carrier wind etc.

moving excitons are optically inactive ($K > K_0 \Rightarrow v > v_s \Rightarrow \text{shock}$)

excitons can travel in a dark state after having been excited
until slowed down to a velocity below photon emission
threshold, where they can decay radiatively

$\longrightarrow$ internal ring

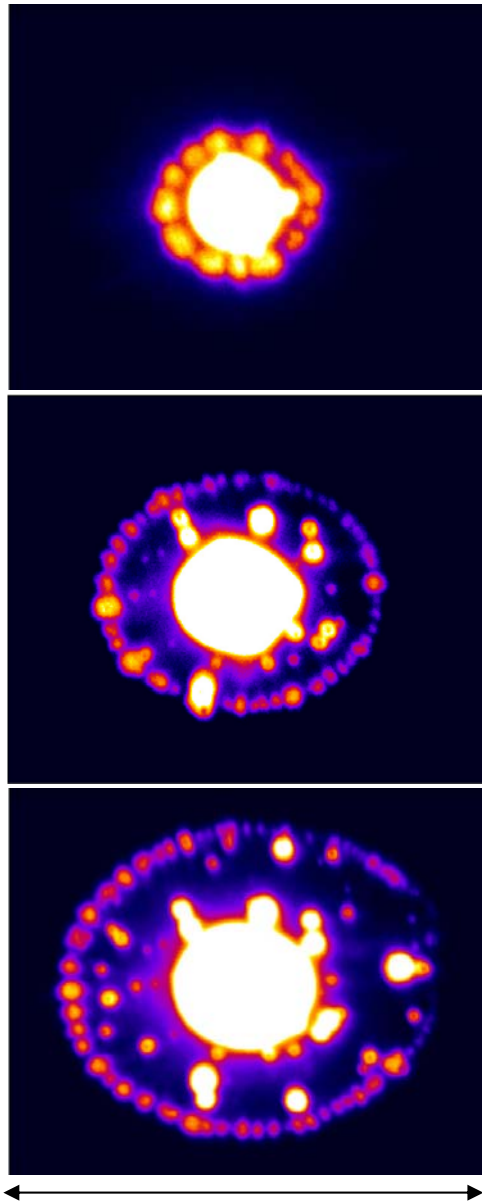
T_x drops outside of excitation spot
fraction of optically active excitons increases

Excitons are generated within the external ring

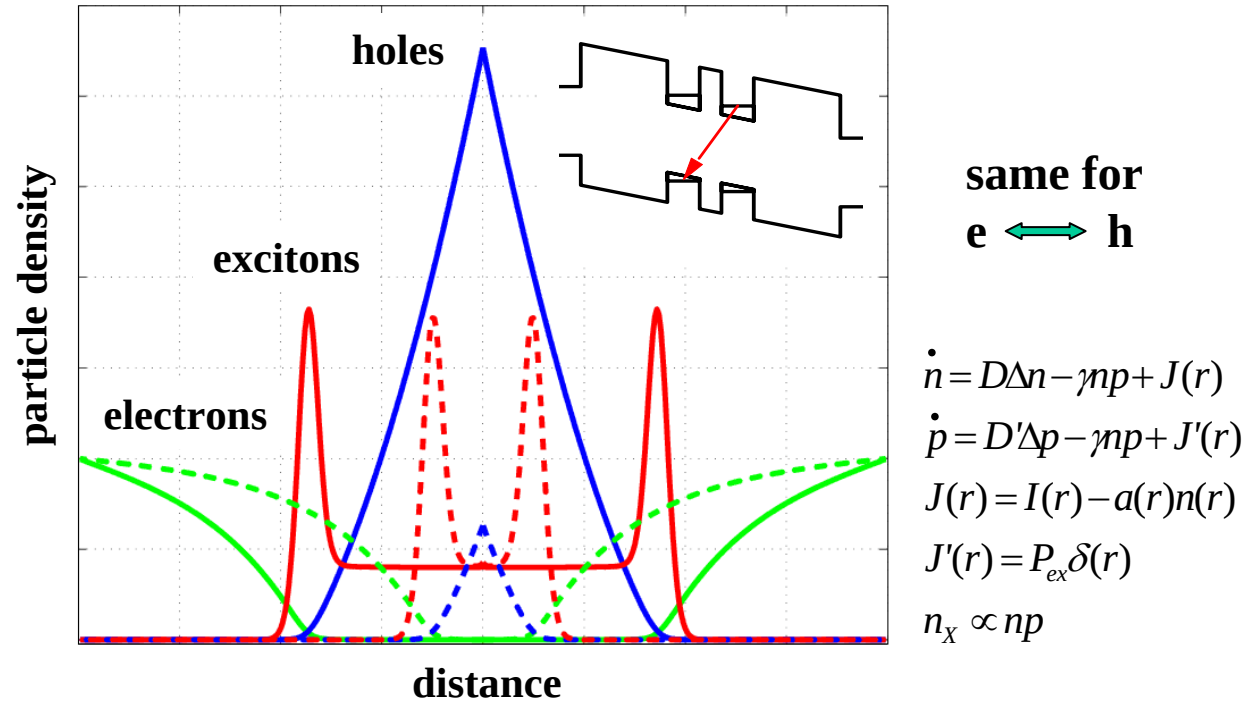
off-resonance laser excitation creates charge imbalance in CQW
electrons and holes have different collection efficiency to CQW

P_{ex}
↓

T=
380
mK



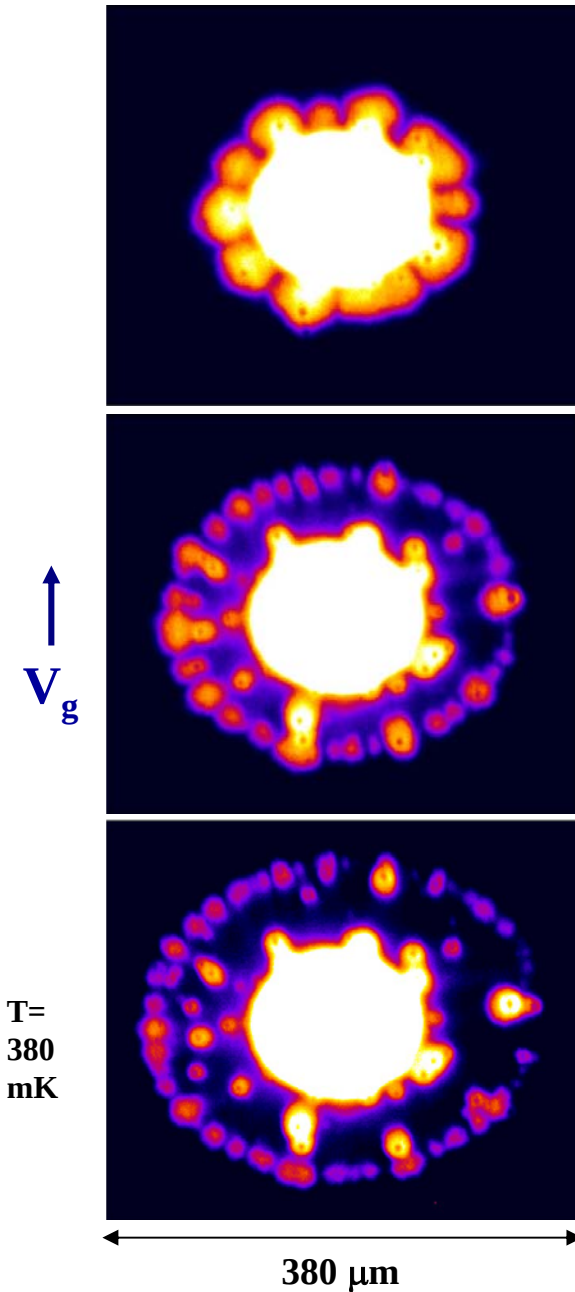
410 μm



holes created at the excitation spot diffuse out
this depletes electrons in the vicinity of the laser spot
creating electron-free and hole rich region

excitons are generated within the
interface between the hole rich region → external ring
and the outer electron rich area

External control of exciton rings



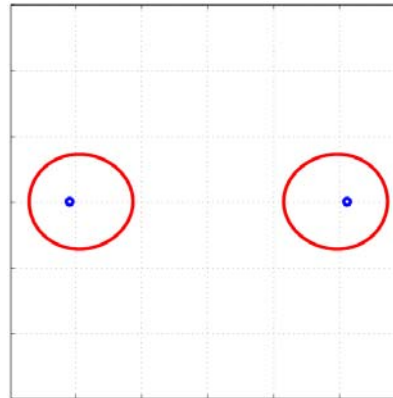
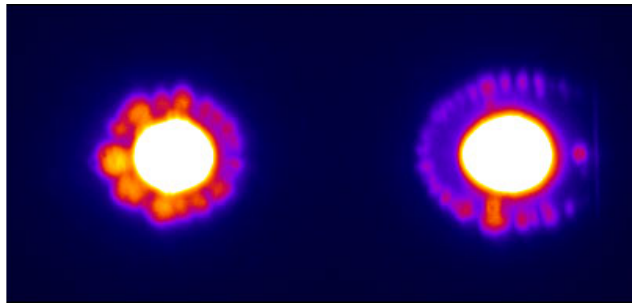
expansion of the ring with decreasing gate voltage



a reduction of transverse electric field, and hence of the current $I(r)$, depletes electrons in CQWs

$$\begin{aligned}\dot{n} &= D\Delta n - \gamma np + J(r) \\ \dot{p} &= D'\Delta p - \gamma np + J'(r) \\ J(r) &= \underline{I(r)} - a(r)n(r) \\ J'(r) &= P_{ex}\delta(r) \\ n_x &\propto np\end{aligned}$$

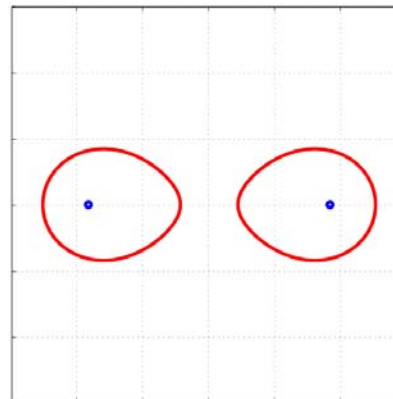
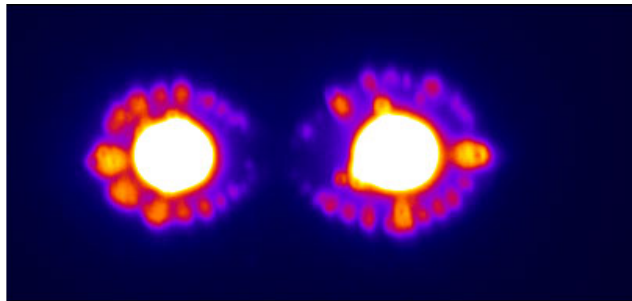
Interaction of two exciton rings



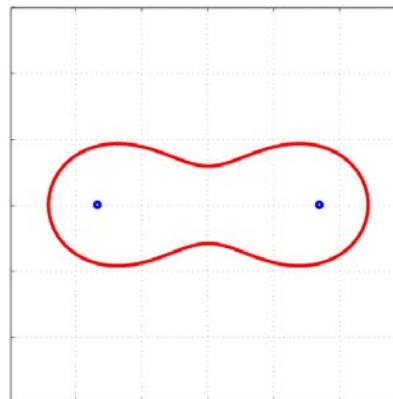
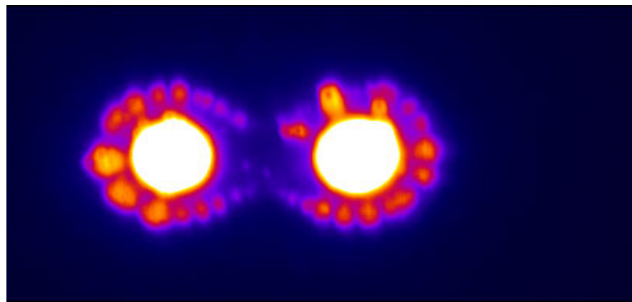
rings attract one another
at large distances



the existence of ``dark matter''
outside the rings that mediates
the interaction



electron flow outside each ring
which is perturbed by the
presence of another ring



electrons in the area between the
rings are depleted more strongly



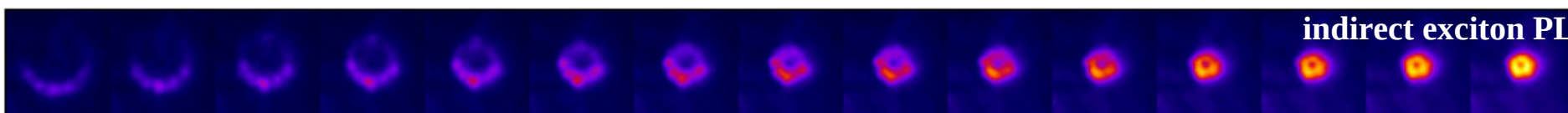
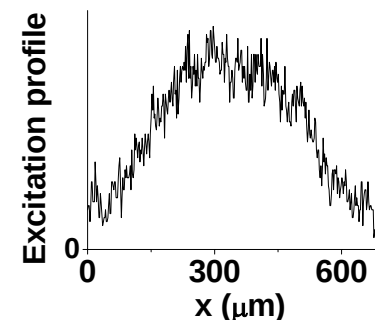
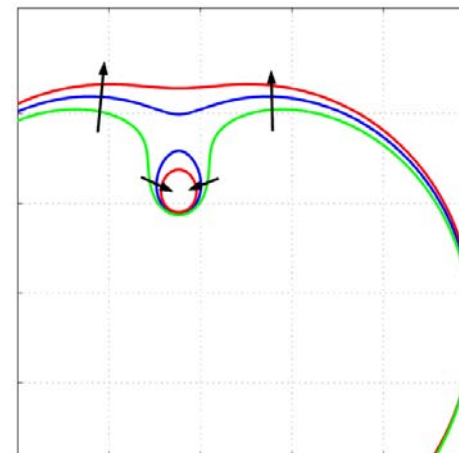
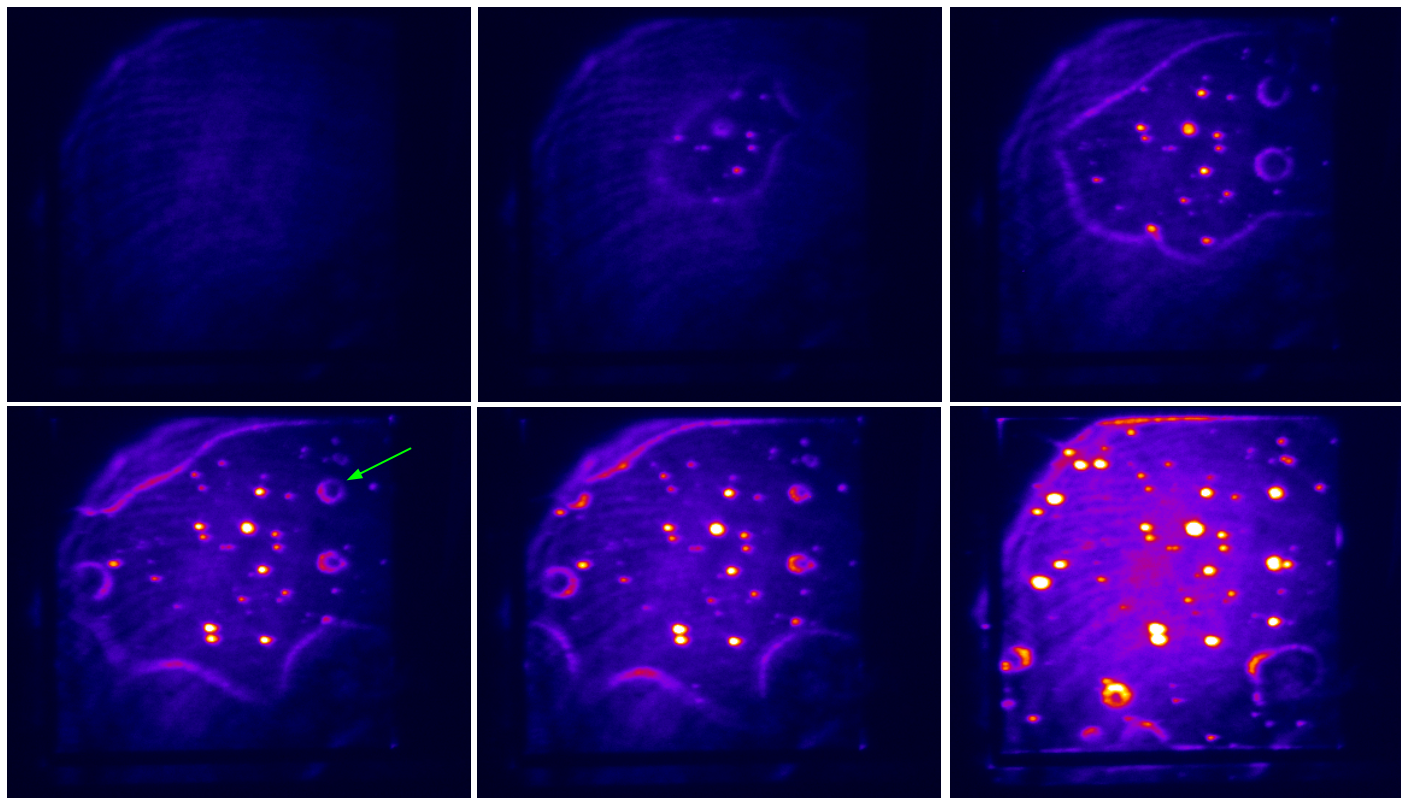
attraction of the rings

T=
380
mK

520 μm

690 μm

Collapse of rings to localized spots



indirect exciton PL



direct exciton PL

$P_{\text{ex}} \longrightarrow$

around the localized spots, small rings appear which shrink at increasing P_{ex}

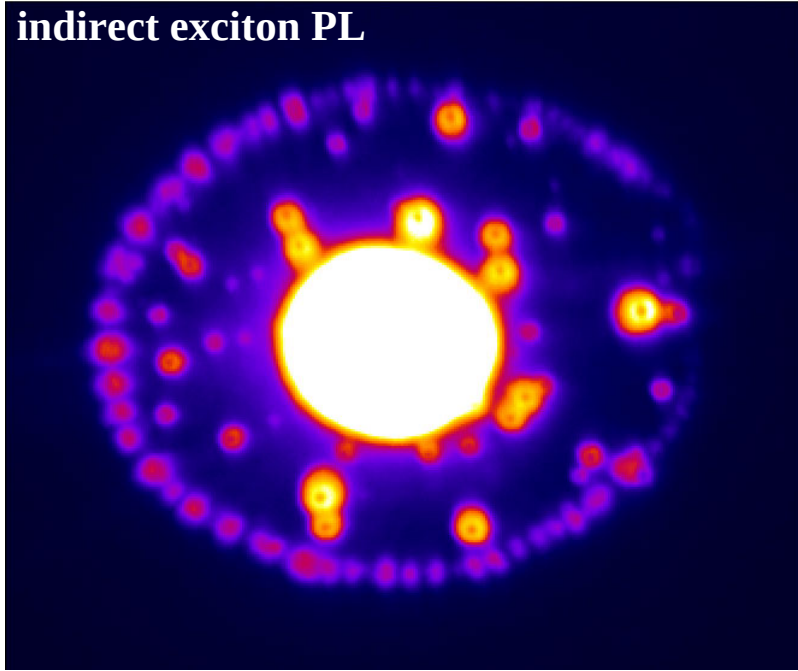
$e \longleftrightarrow h$

localized sources of electrons (due to pinholes) embedded in the hole rich illuminated area

direct exciton emission indicates hot cores at the center of the collapsed rings

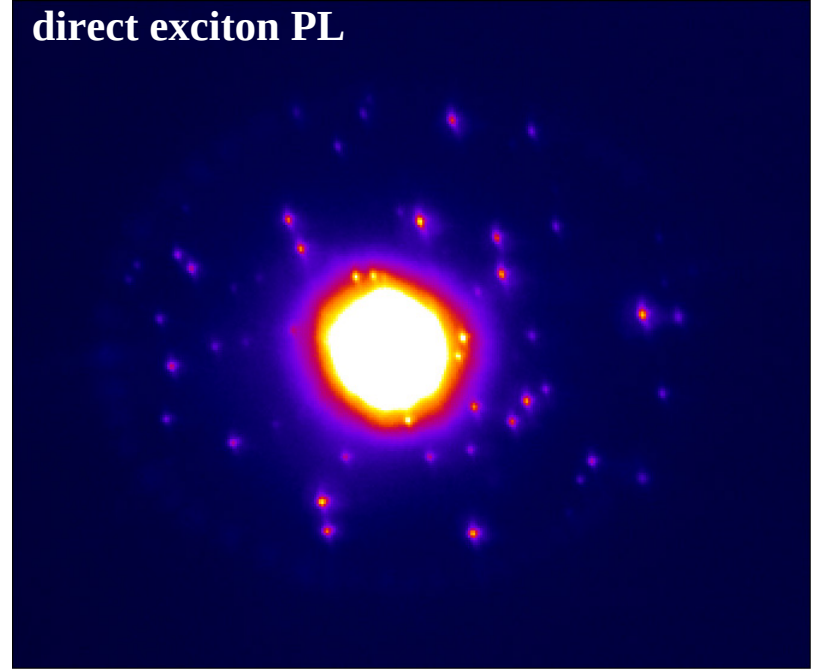
Ordered phase

indirect exciton PL



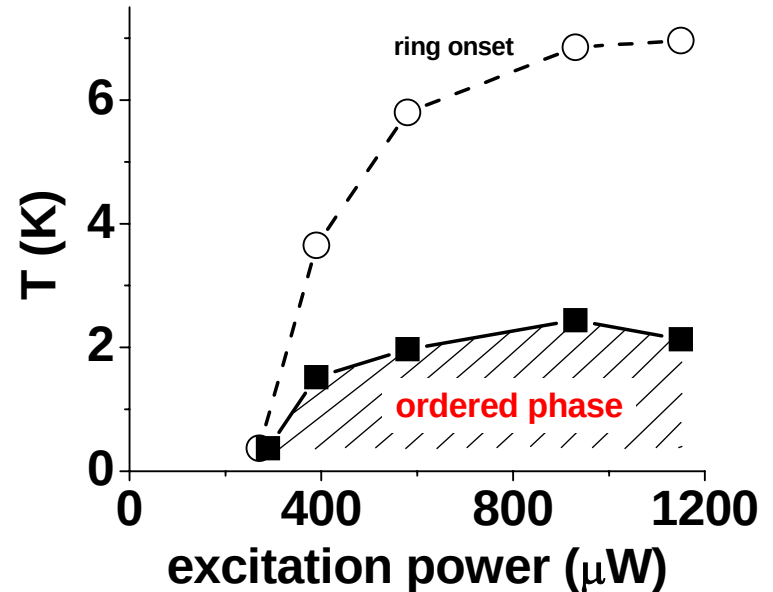
410 μm

direct exciton PL



aggregates on the ring have no hot cores contrary to bright spots generated by the pinholes

aggregates move in concert with the ring when the position of the source is adjusted showing further that in-plane potential fluctuations are not strong enough to destroy the ordering



the rings represent a source of cold excitons
with a temperature close to that of the lattice
in external ring heating sources vanish → exciton gas is the coldest



macroscopically ordered exciton state

macroscopically ordered phases can be both in
quantum (e.g. atom BEC)
and classical (e.g. Taylor vortices) systems

↑
new state, not predicted

↑
microscopic nature of
ordered exciton state - ?

the macroscopically ordered phase appears abruptly at low temperatures
is observed in the same temperature range as bosonic stimulation of exciton scattering



statistically degenerate Bose-gas of excitons



the macroscopic ordering is an intrinsic
property of exciton condensate ?

Similarities with known phenomena: Modulational instabilities

stationary solutions to 1D nonlinear Schrodinger equation under periodic boundary conditions



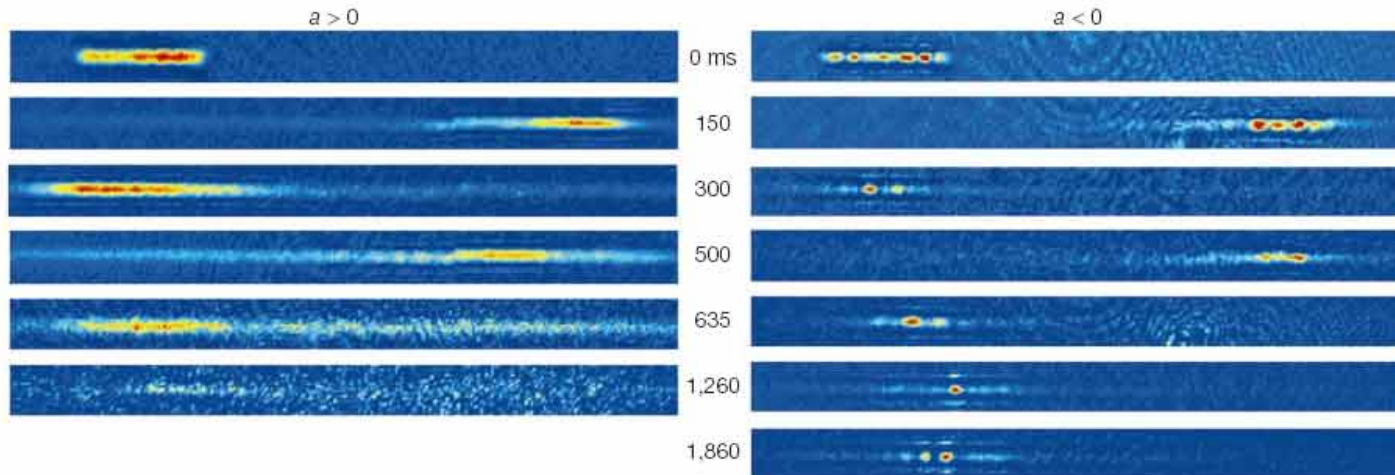
stationary soliton trains

on a ring

experimental example:

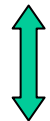
soliton train in atom BEC with attractive interaction

K.E. Strecker, G.B. Partridge, A.G. Truscott, R.G. Hulet, Nature 417, 150 (2002)



soliton train
is observed
below T_c only
↓
intrinsic
property of
atom BEC

repulsion between beads of soliton train is wave interference phenomenon



attractive interaction
for indirect excitons ?

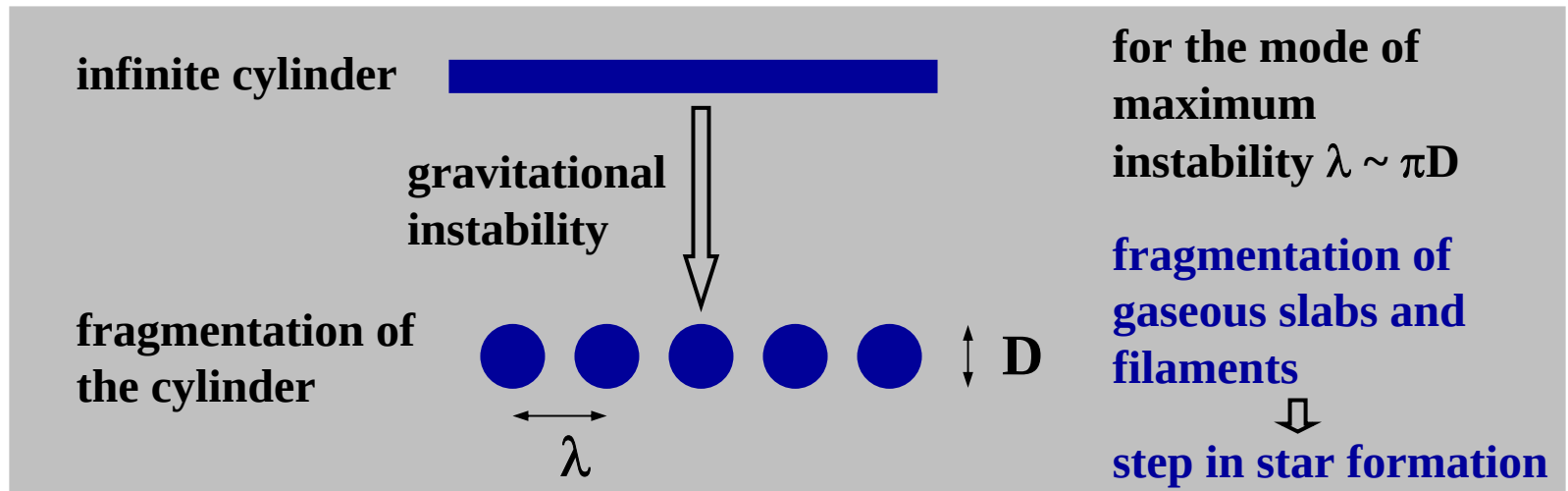
the macroscopic ordering is an intrinsic
property of exciton condensate ?

Similarities in astrophysics

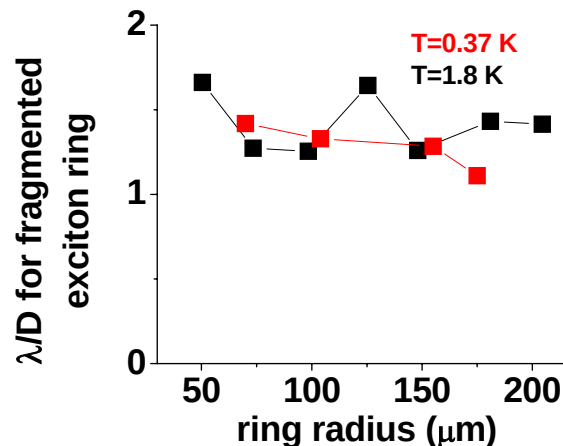
S. Chandrasekhar and E. Fermi (1953)

gravitational instability of an infinite cylinder:

the cylinder is unstable for all modes of deformation with wavelengths exceeding a certain critical value



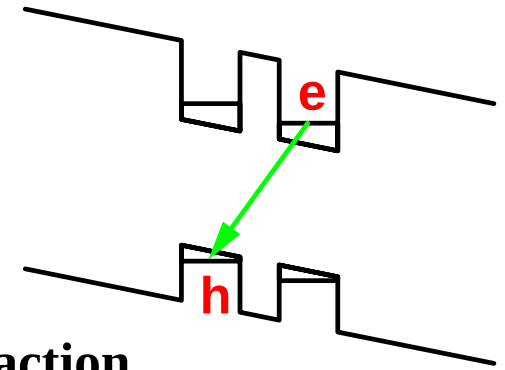
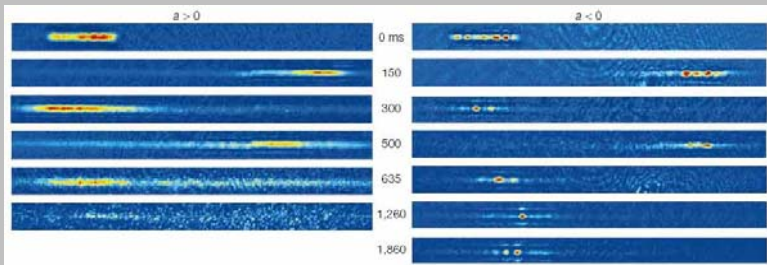
**attractive interaction
for indirect excitons ?**



attractive interaction ?

soliton train in atom BEC appears when the interaction is switched from repulsive to attractive

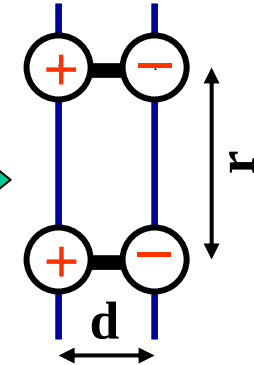
K.E. Strecker et al., Nature 417, 150 (2002)



dipole-dipole interaction

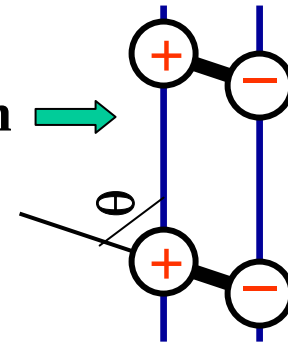
$$U \sim d^2/r^3 (1-3\cos^2\theta)$$

repulsive interaction



attractive interaction

(for $\cos^2\theta < 1/3$)

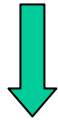


when in-plane electric field exceeds the threshold the interaction switches from repulsive to attractive ?

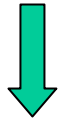
indirect excitons with spatially separated
electrons and holes, $d_{eh} \sim 10$ nm



strong dipole-dipole interaction
large in-plane polarizability



spontaneous in plane dipole alignment
at $T < T_c$



instability due to attractive interaction

?

