

# *Two Channel Kondo in a Modified SET*

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[http://www.weizmann.ac.il/condmat/oreg\\_group.html](http://www.weizmann.ac.il/condmat/oreg_group.html)

# *Outline*

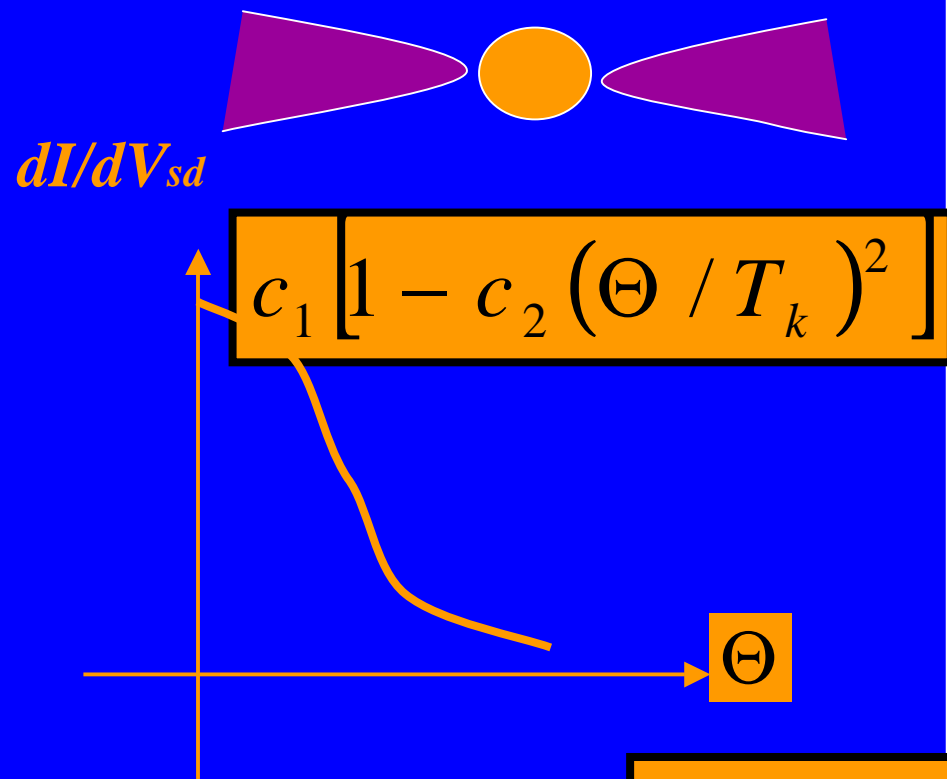
- Fermi liquid vs. non Fermi Liquids (NFL).
- Fermi edge singularity (FES).
- Single channel Kondo effect – Schrieffer-Wolff and Coulomb gas.
- Multi-channel Kondo effect an academic exercise (Nozieres ,Blandin and Zawadowski).
- Realization of multi-channel Kondo effect (MCK) in a single electron transistor (SET).
- Possible measurements of MCK in a SET.
- Summary.

# 2-Channel Vs 1-Channel Kondo

$T \ll T_K$	Single Channel	Two Channel
Entropy	$a \frac{T}{T_K} \xrightarrow{T \rightarrow 0} 0 = \text{Log}[1]$	$\frac{1}{2} \text{Log} [2]$
Spin Susceptibility	$b \frac{(g\mu_B)^2}{T_K}$	$\beta \frac{(g\mu_B)^2}{T_K} \text{Log} \left( \frac{T_K}{T} \right)$
Specific Heat	$a \frac{T}{T_K}$	$\alpha \left( \frac{T}{T_K} \right) \text{Log} \left( \frac{T_K}{T} \right)$
Conductance	$c_1 - c_2 \left( \frac{T}{T_K} \right)^2$	$\gamma_1 \pm \gamma_2 \sqrt{\frac{T}{T_K}}$

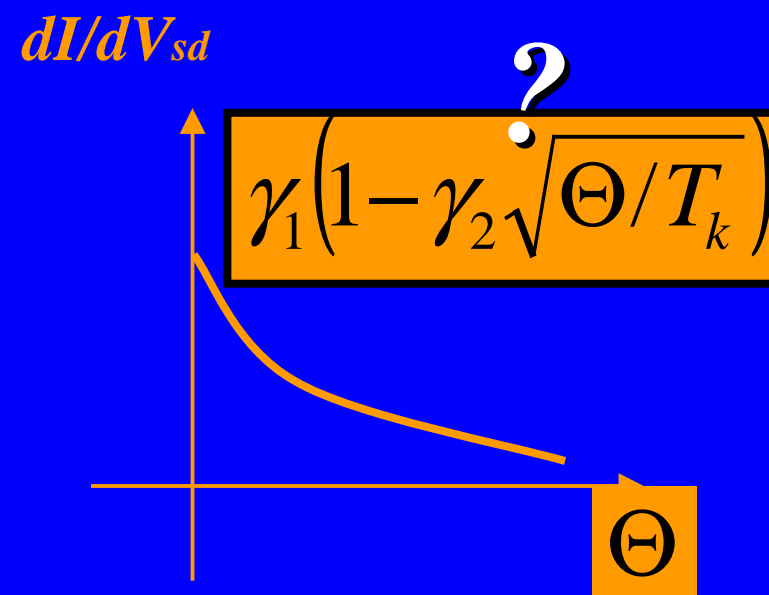
## *Fermi Liquid (FL)*

### Single Channel Kondo



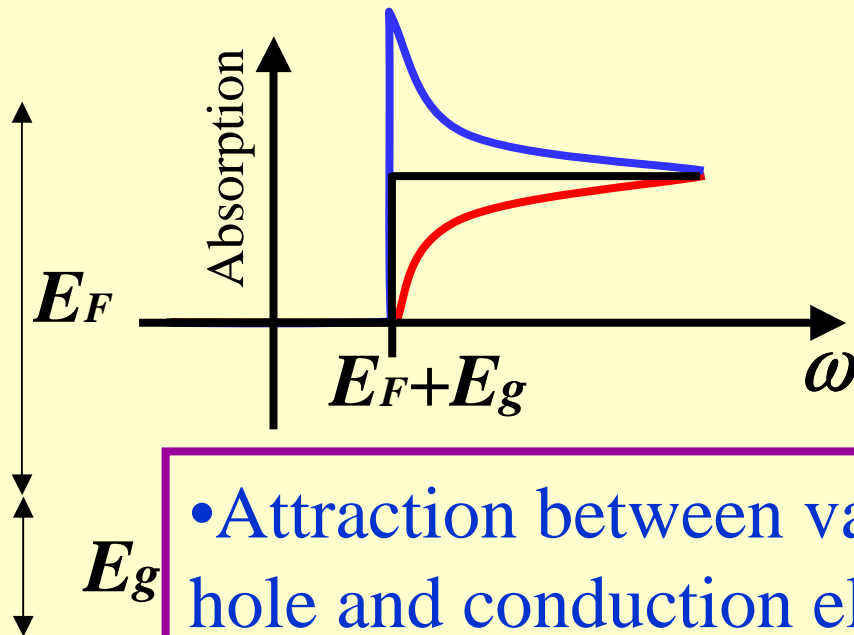
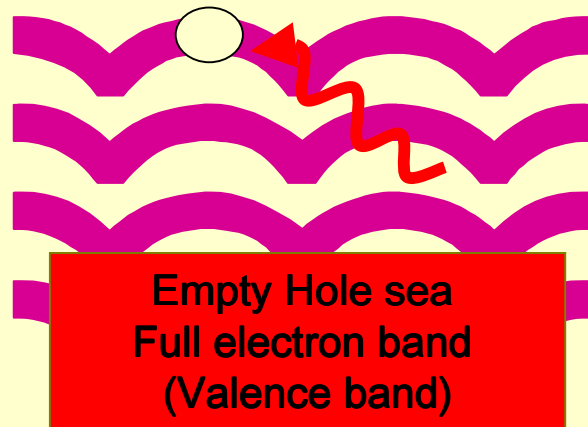
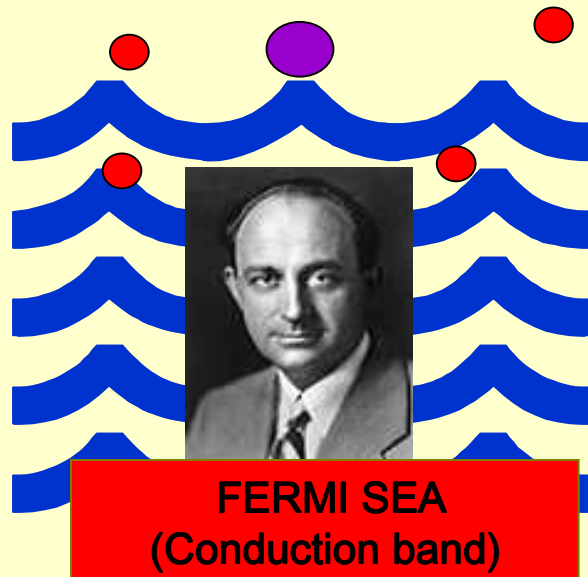
## *Non FL*

### Two-Channel Kondo



$$\Theta \equiv \max[T, V_{sd}]$$

# *Fermi Edge singularity*



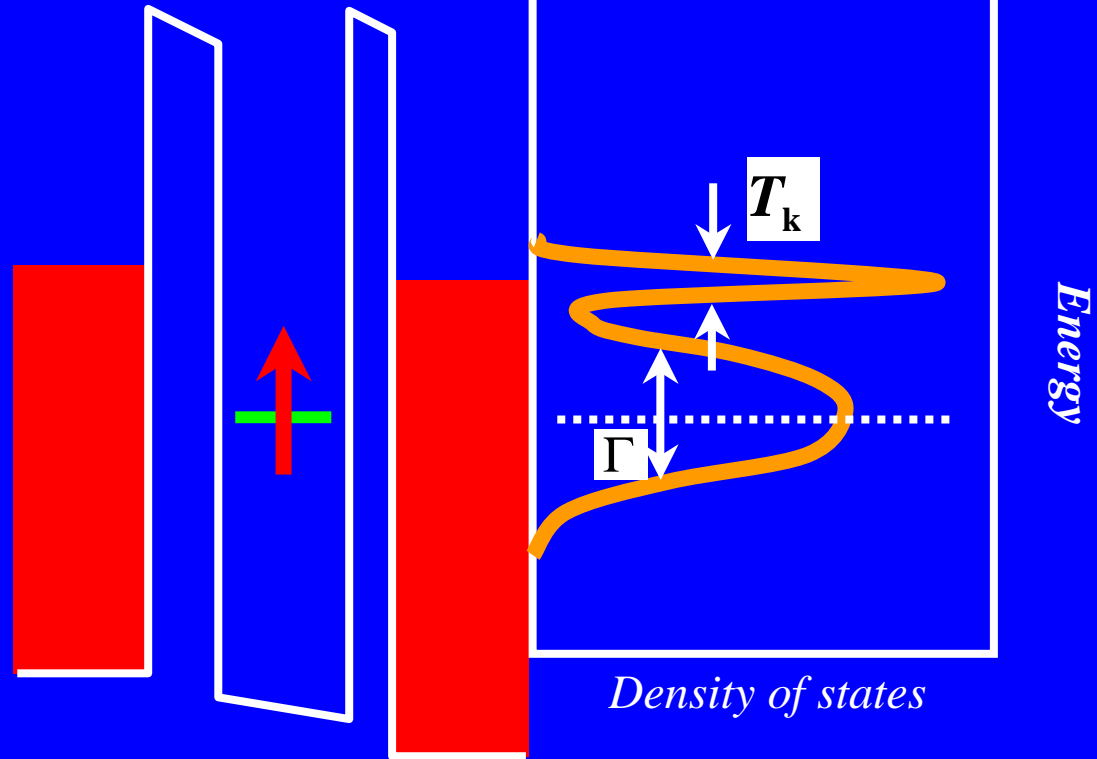
- Attraction between valance hole and conduction electrons.
- Orthogonality “catastrophe”

Sudden potential +  
Many body effects

# *Single Channel Kondo and Anderson Model: Many FES*



Jun Kondo

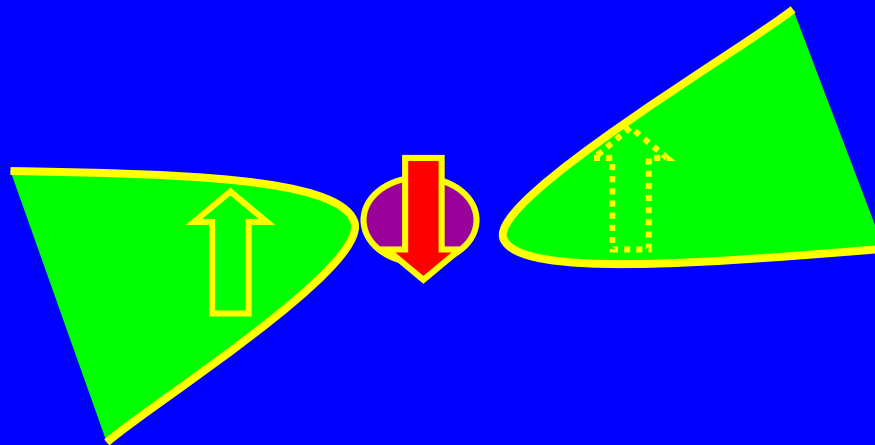


# *Spin – Charge Separation*

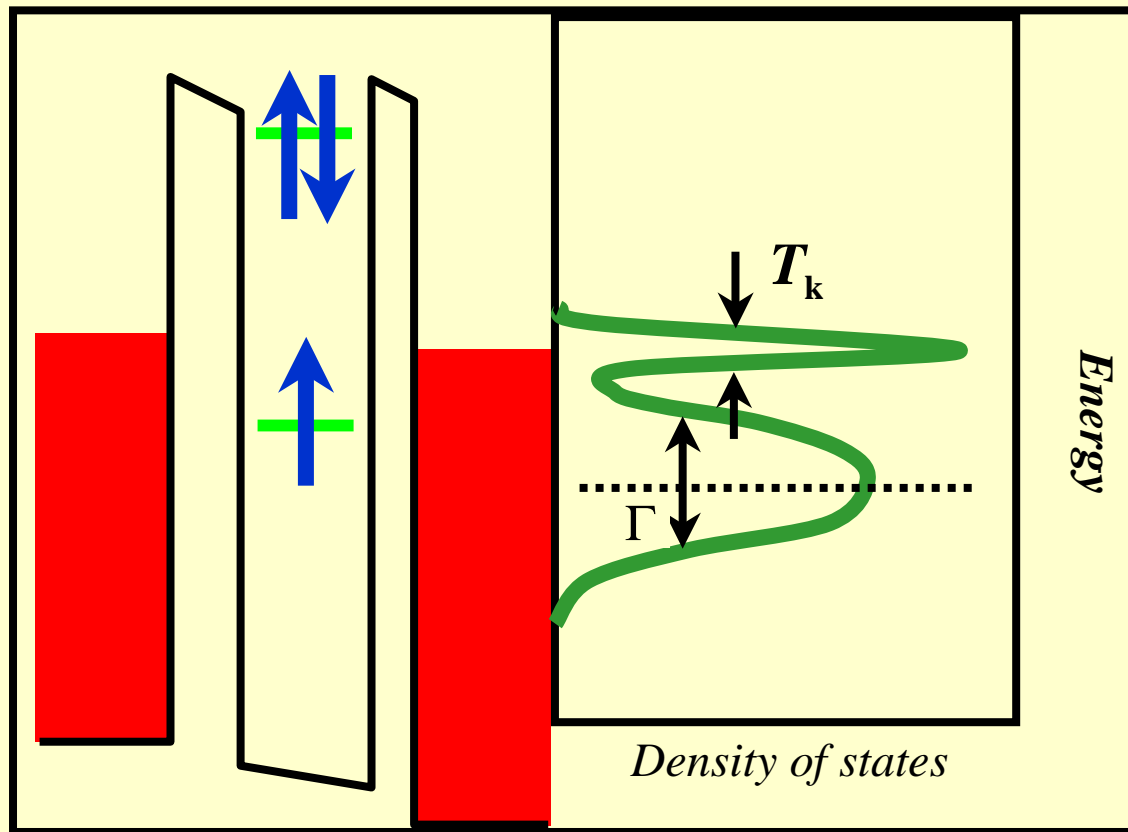
Conduction spin

Dot spin

$$J \vec{\sigma} \cdot \vec{S}, \quad J > 0$$



*Anderson  $\rightarrow$  Haldane  $\rightarrow$  Schrieffer-  
Wolff  $\rightarrow$  Kondo  $\rightarrow$  Resonance*





# *Anderson Model*

$$H = \sum_{ks} \varepsilon_{ks} l_{ks}^+ l_{ks} + \sum_s \varepsilon_d^0 d_s^+ d_s + U n_{d\uparrow} n_{d\downarrow} \\ + \sum_{ks} \left( v_{lk}^* l_{ks}^+ d_s + V_{lk} d_s^+ l_{ks} \right)$$

# *Schrieffer-Wolff*

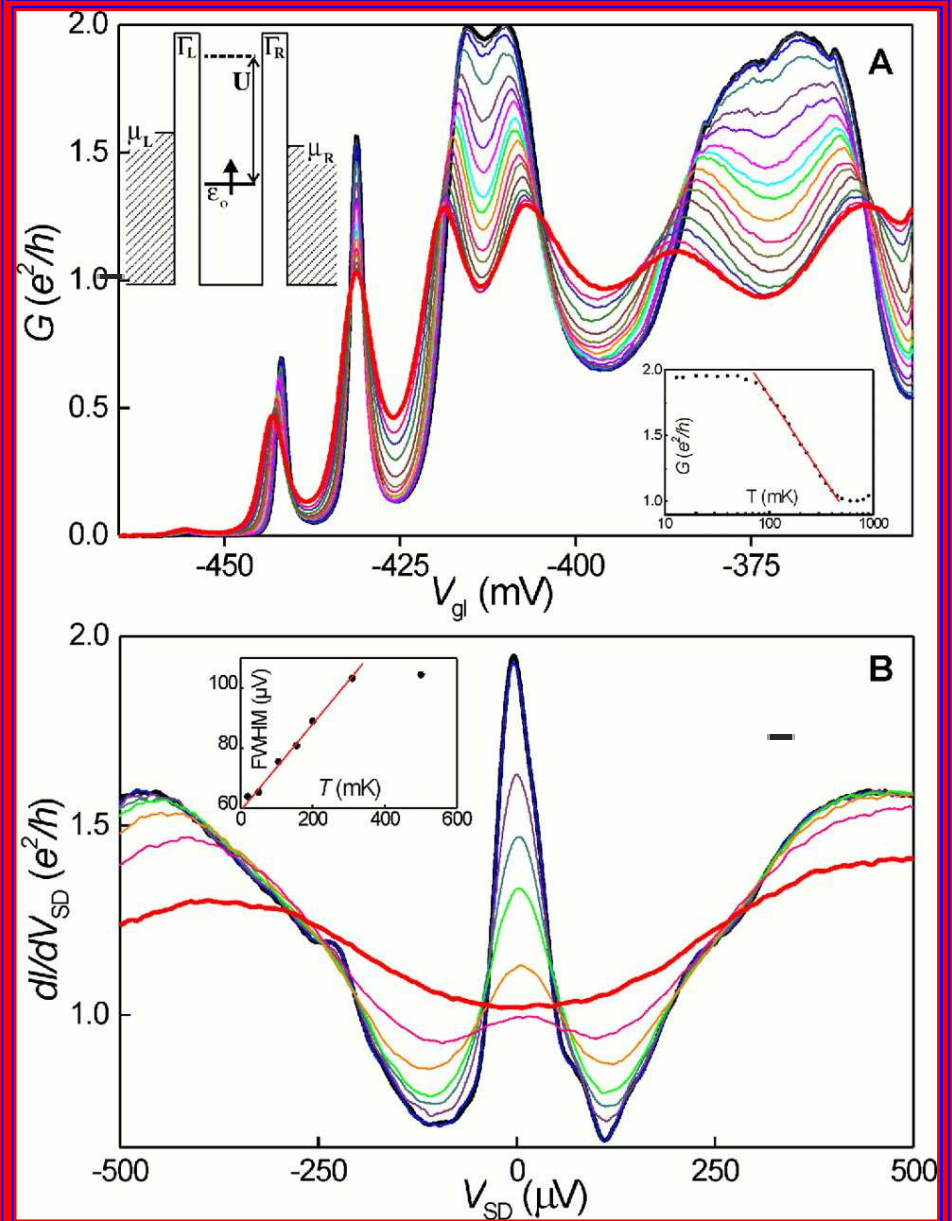
$$H = \sum_{ks} \varepsilon_{ks} l_{ks}^+ l_{ks} + \sum_{kq} J^{kq} \left[ S^+ s^{-kq} + S^- s^{+kq} + 2S^z s^{zkq} \right]$$

$$S^+ = d_{\uparrow}^+ d_{\downarrow}, S^- = d_{\downarrow}^+ d_{\uparrow}, S^z = \frac{1}{2} (d_{\uparrow}^+ d_{\uparrow} - d_{\downarrow}^+ d_{\downarrow}),$$
$$S^{+kq} = l_{k\uparrow}^+ l_{q\downarrow}, S^{-kq} = l_{k\downarrow}^+ l_{q\uparrow}, S^{zkq} = \frac{1}{2} (l_{k\uparrow}^+ l_{q\uparrow} - l_{k\downarrow}^+ l_{q\downarrow})$$

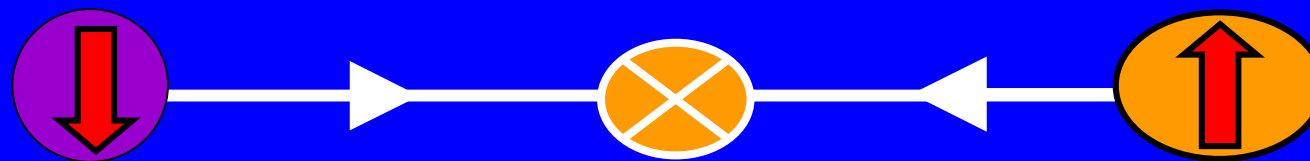
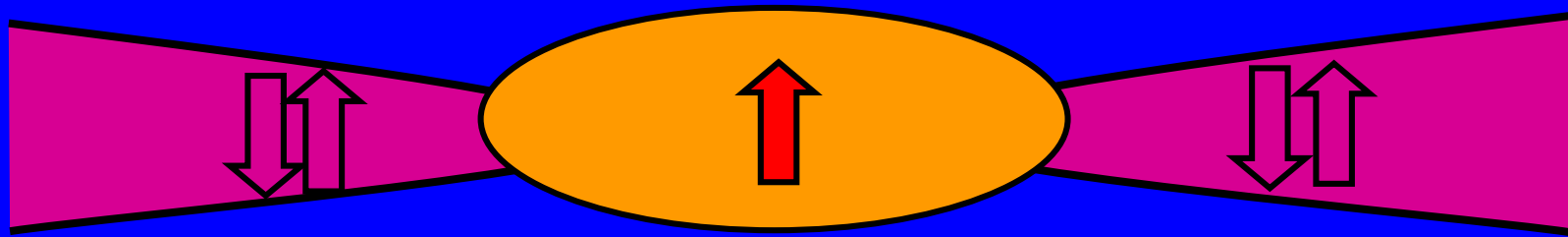
$$J^{kq} = V_k V_q^* \left[ \frac{1}{E_{\text{elec}} - E_{\text{init}}} + \frac{1}{E_{\text{hole}} - E_{\text{init}}} \right]$$

(A) Coulomb oscillations in  $G$  versus  $V_{\text{gl}}$  at  $B = 0.4$  T for different temperatures.  $T$  ranges from 15 mK (thick black trace) up to 800 mK (thick red trace).  $V_{\text{gr}}$  is fixed at 448 mV. The red line in the right inset highlights the logarithmic  $T$  dependence between  $\sim 90$  and  $\sim 500$  mK for  $V_{\text{gl}} = -413$  mV. The left inset explains the variables used in the text with  $\Gamma \equiv \Gamma_L + \Gamma_R$ .  $\varepsilon_0$  is negative and measured from the Fermi level in the leads at equilibrium.

(B) Differential conductance  $dI/dV_{\text{SD}}$  versus dc bias voltage between source and drain contacts  $V_{\text{SD}}$  for  $T$  ranging from 15 mK (thick black trace) up to 900 mK (thick red trace), at  $V_{\text{gl}} = -413$  mV and  $B = 0.4$  T. The inset shows that the width of the zero-bias peak, measured from the FWHM, increases linearly with  $T$ . The red line indicates a slope of  $1.7 k_B/e$ . At 15 mK, the FWHM = 64  $\mu\text{V}$ , and it starts to saturate around 300 mK.

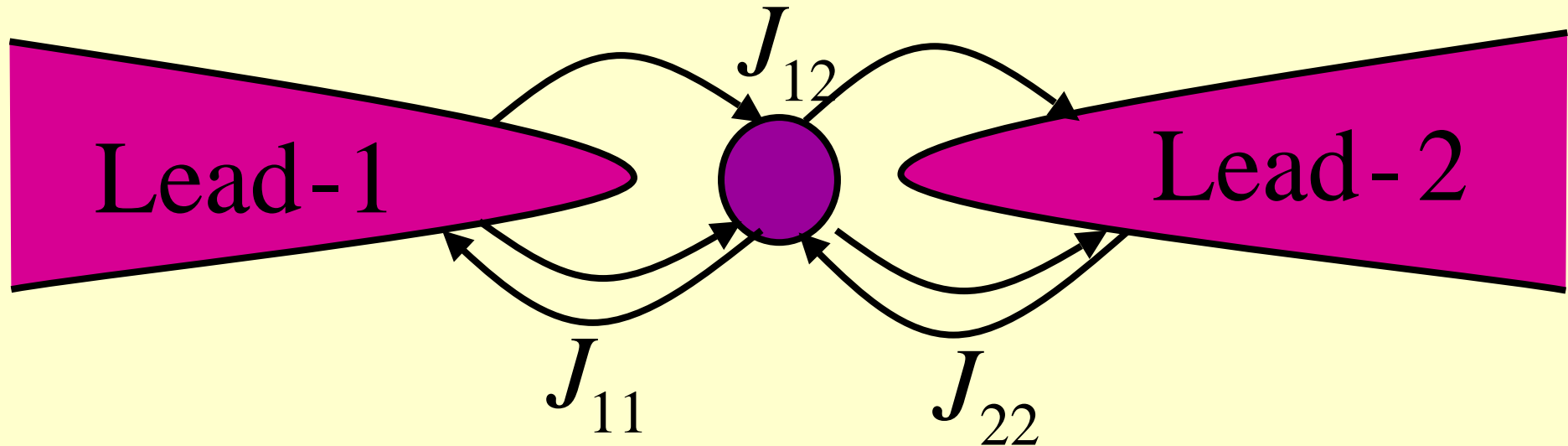


# *Multi - Channel Kondo*



- RG, NRG
- Bethe Ansatz (Andrei, Wiegmann-Tsvelik)
- Conformal Field Theory (Affleck - Ludwig)
- “Pseudo Particle” or “Slave Bosons”  
(Read - Coleman, Ruckenstein - Cox)
- Bosonization (Kivelson - Emery)

# *Channel anisotropy*



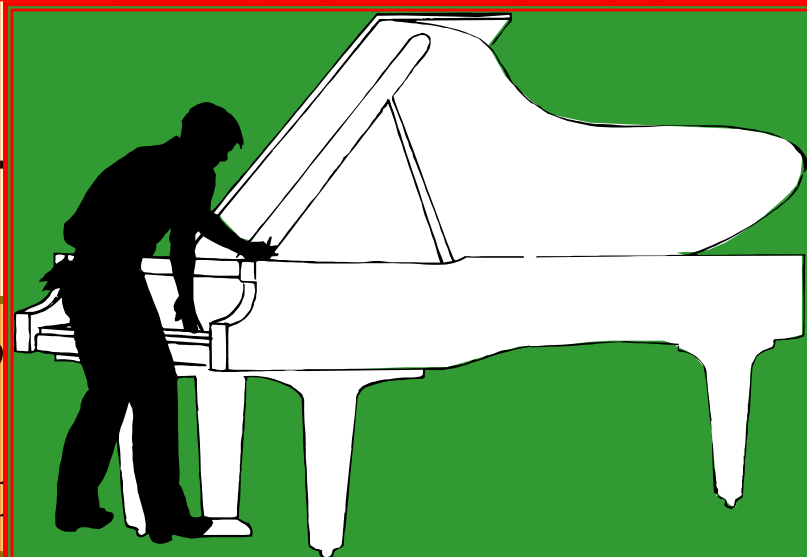
$$\begin{pmatrix} J_{11} & J_{12} \\ J_{21} & J_{22} \end{pmatrix} \Rightarrow \begin{pmatrix} J_1 & 0 \\ 0 & J_2 \end{pmatrix} =$$

$$\frac{1}{2} \begin{pmatrix} J_{11} - J_{22} + \sqrt{(J_{11} - J_{22})^2 + 4J_{12}J_{21}} & 0 \\ 0 & J_{11} - J_{22} - \sqrt{(J_{11} - J_{22})^2 + 4J_{12}J_{21}} \end{pmatrix}$$

*In Quantum dots  
we can tune*

$$J_1 = J_2$$

$m = 1, 2$  and  $p$   
 $\tilde{J} = J \bullet \text{Dens}$



1CK

$$) = \tilde{J}_m^2 - \tilde{J}_m \sum_p \tilde{J}_p^2.$$

# *Suggestions for 2CK Realizations:*

**~100 Publications/attempts to realize MCK**

- Two level systems, “spins are isotropic channels”
  - Theo: Zawadowski, von Delft et al,
  - Exp: Dan Ralph and Burman.
- Coulomb blockade peak is a degenerate state
  - The. Matveev et al. (Requires a large dot, and smooth contacts)
  - Exp. Devoret et al.  $\Delta \ll T_k \approx \sqrt{E_c \Gamma} e^{-E_c/\Gamma} \ll E_c$  Hard in real systems.
  - Schiller et al.
- Quadruple 2CK (**Cox**)
- Non equilibrium (**Wen**)
- Luttinger leads (**Kim**)

Charging energy

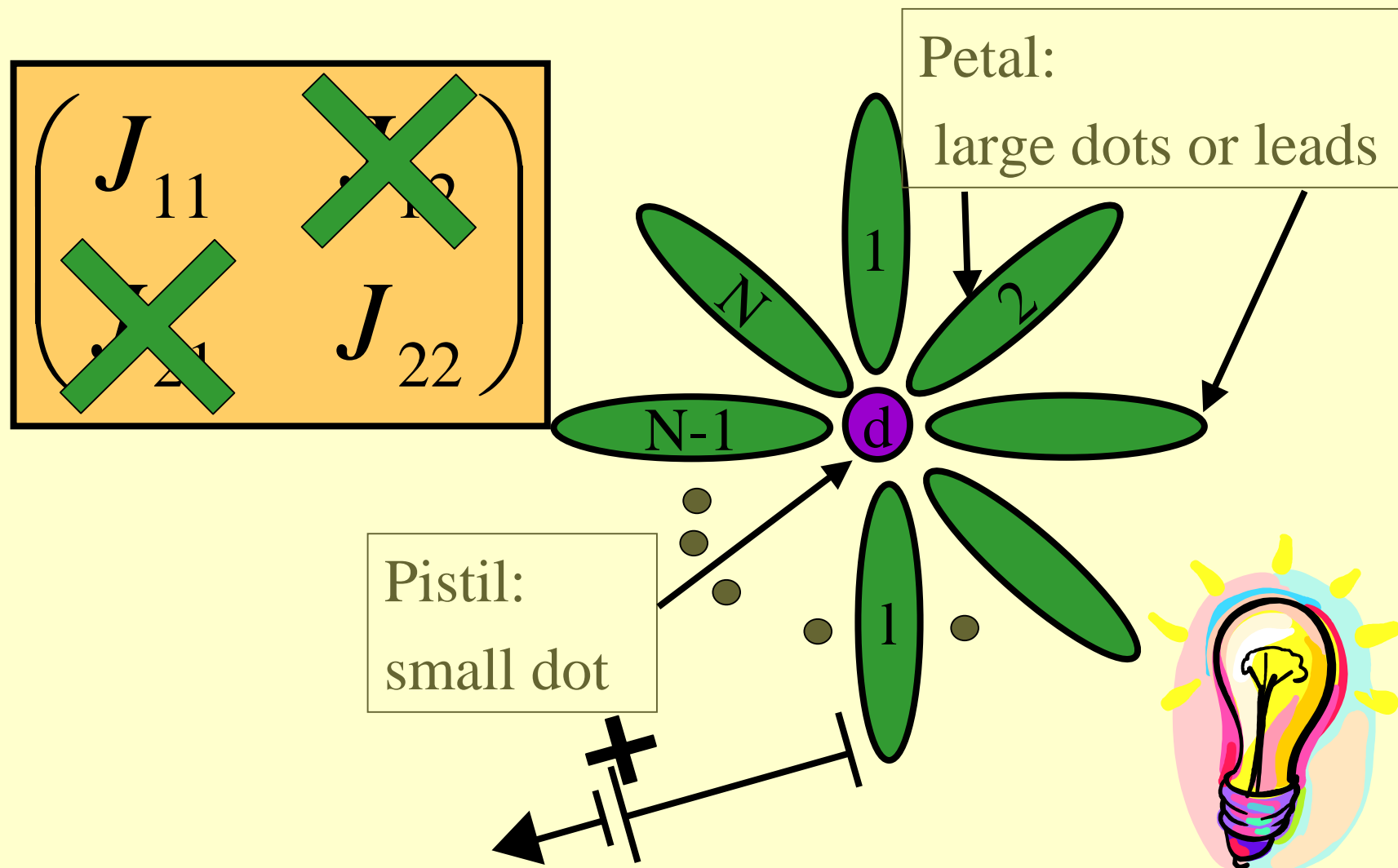
Lead-Dot Coupling const

Kondo temp.

Average level spacing

# A simple realization of MCK

YO and David Goldhaber-Gordon



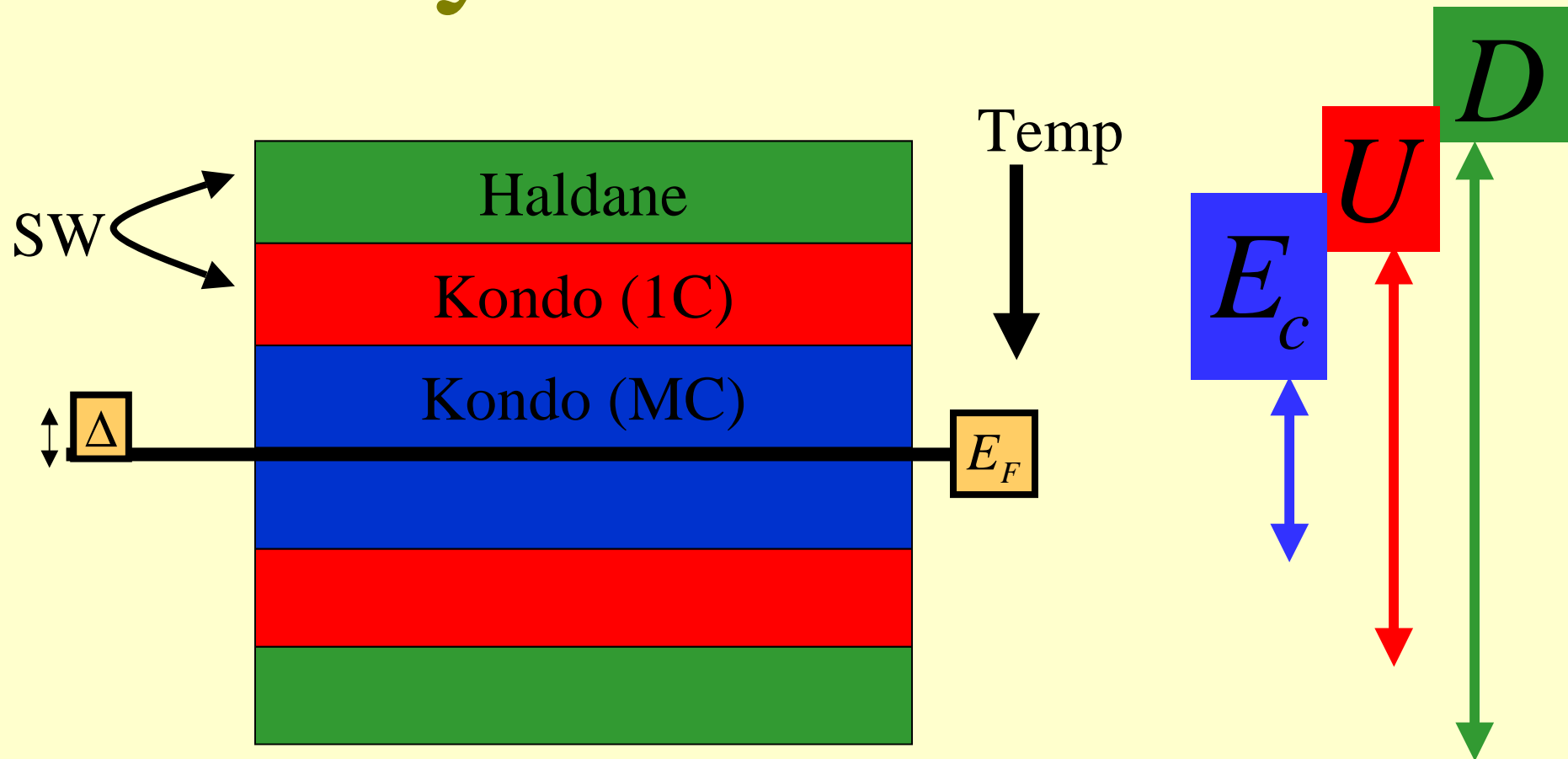


# Generalized Anderson Model

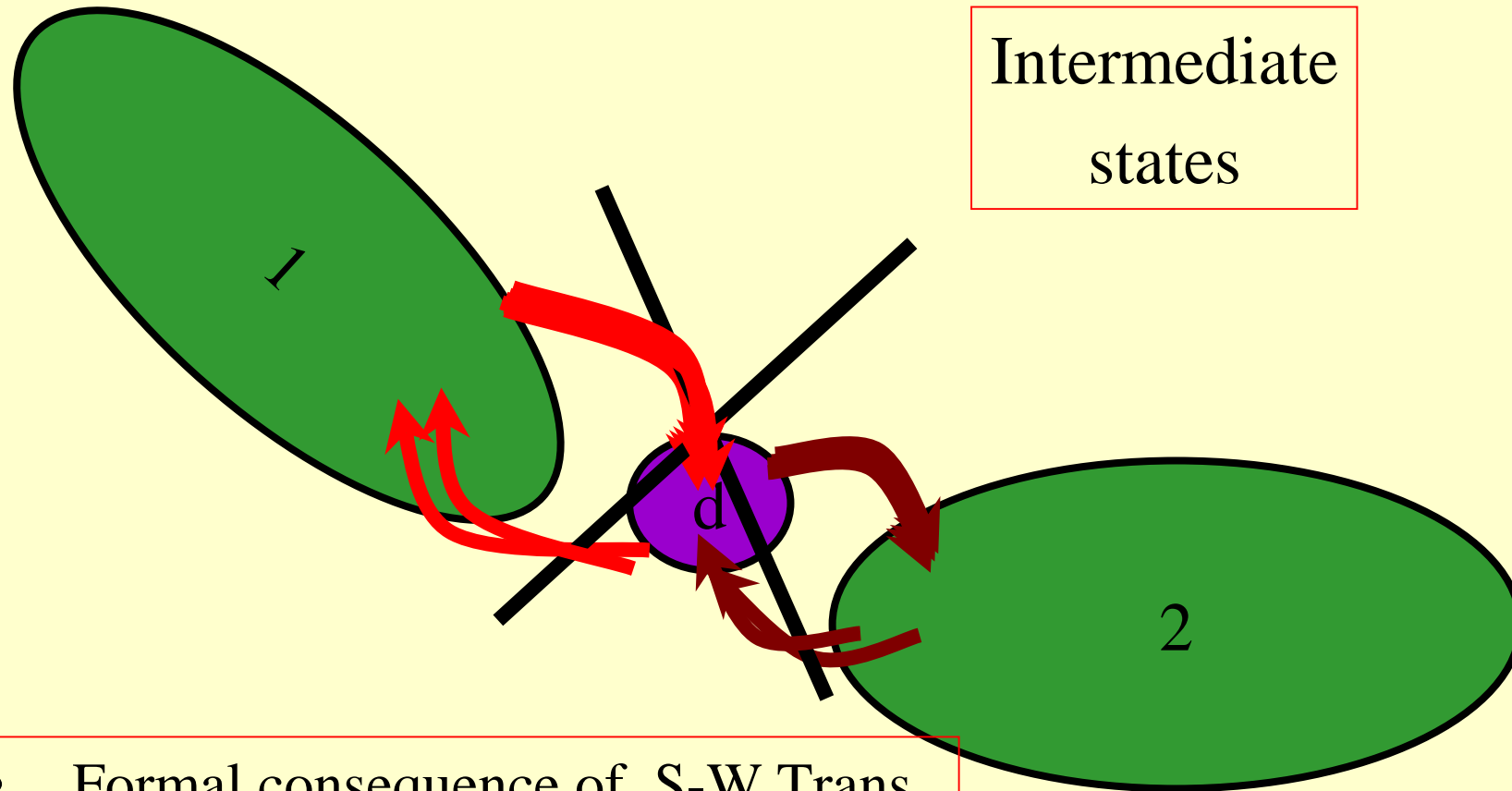
$$\begin{aligned}
 H = & \sum_{kls} \varepsilon_{ks} l_{ks}^+ l_{ks} + \sum_s \varepsilon_d^0 d_s^+ d_s + U n_{d\uparrow} n_{d\downarrow} \\
 & + \sum_l E_{cl} (n_l - N_l)^2 \\
 & + \sum_{ks} (v_{lk}^* l_{ks}^+ d_s + v_{lk} d_s^+ l_{ks})
 \end{aligned}$$

- Charging energy of large-dot-1
- Gate potential on large-dot-1
- Number of electrons in large-dot-1

# Analysis of the model

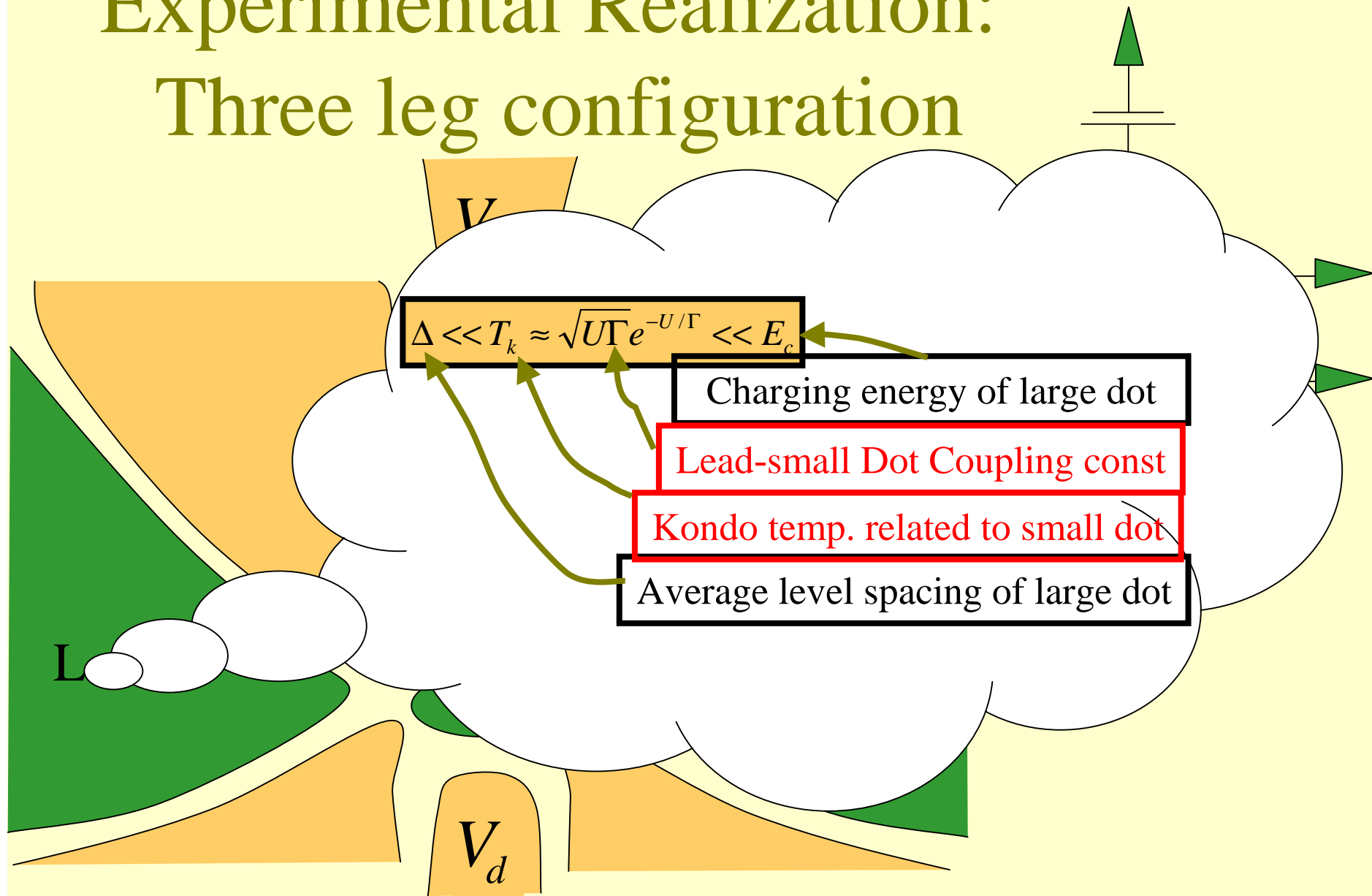


# Neglect Higher Orders

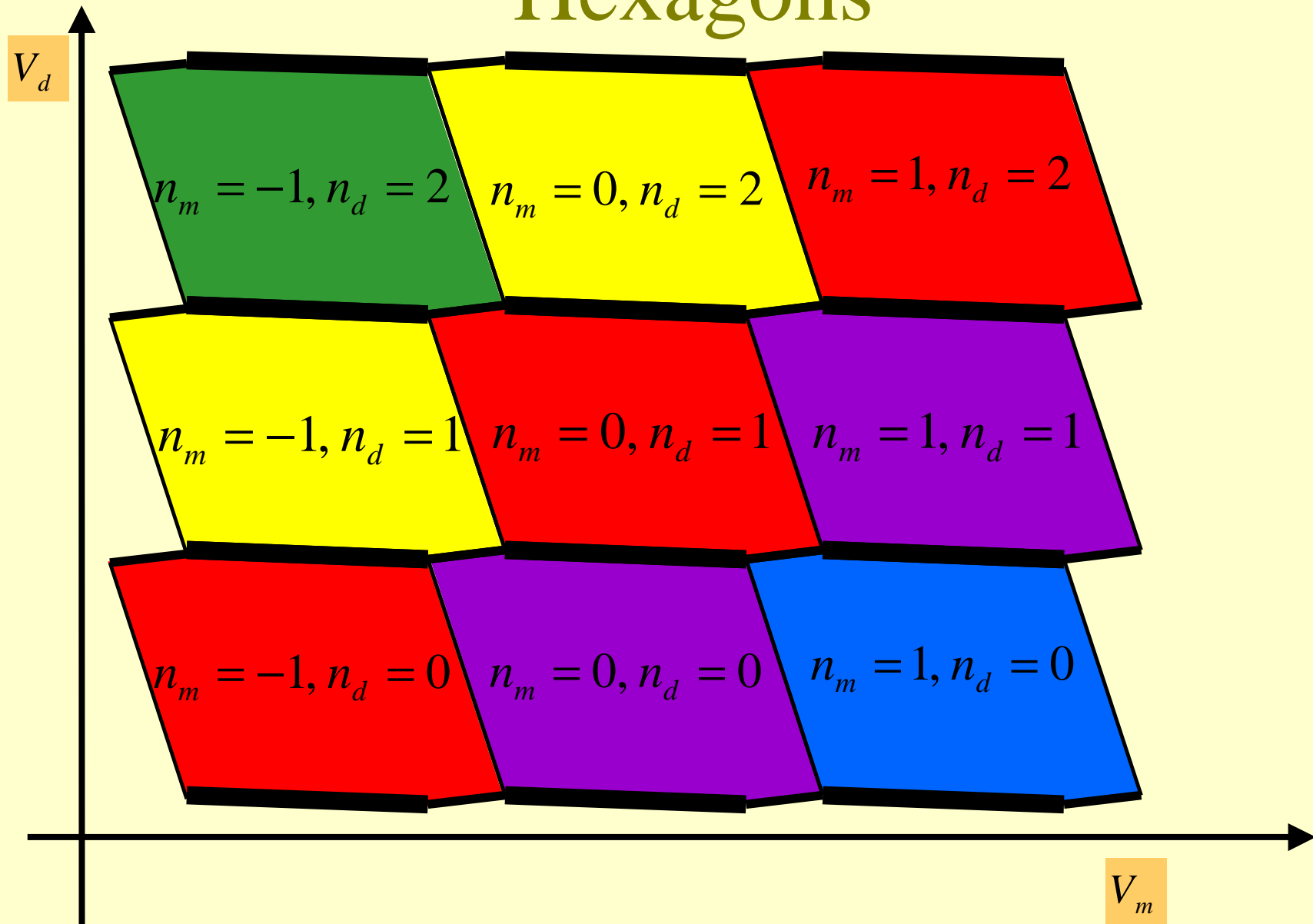


- Formal consequence of S-W Trans  
Coqblin & Schrieffer (1969)
- Smaller by a Factor  $U/T$  compare to  
two separate hops to the same dot

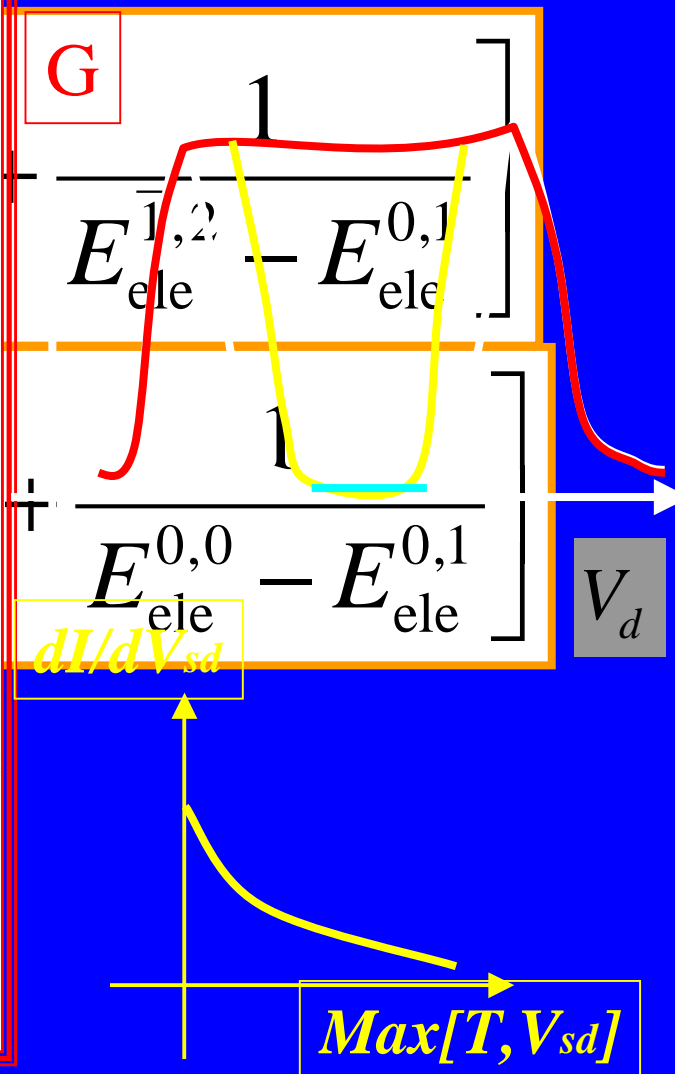
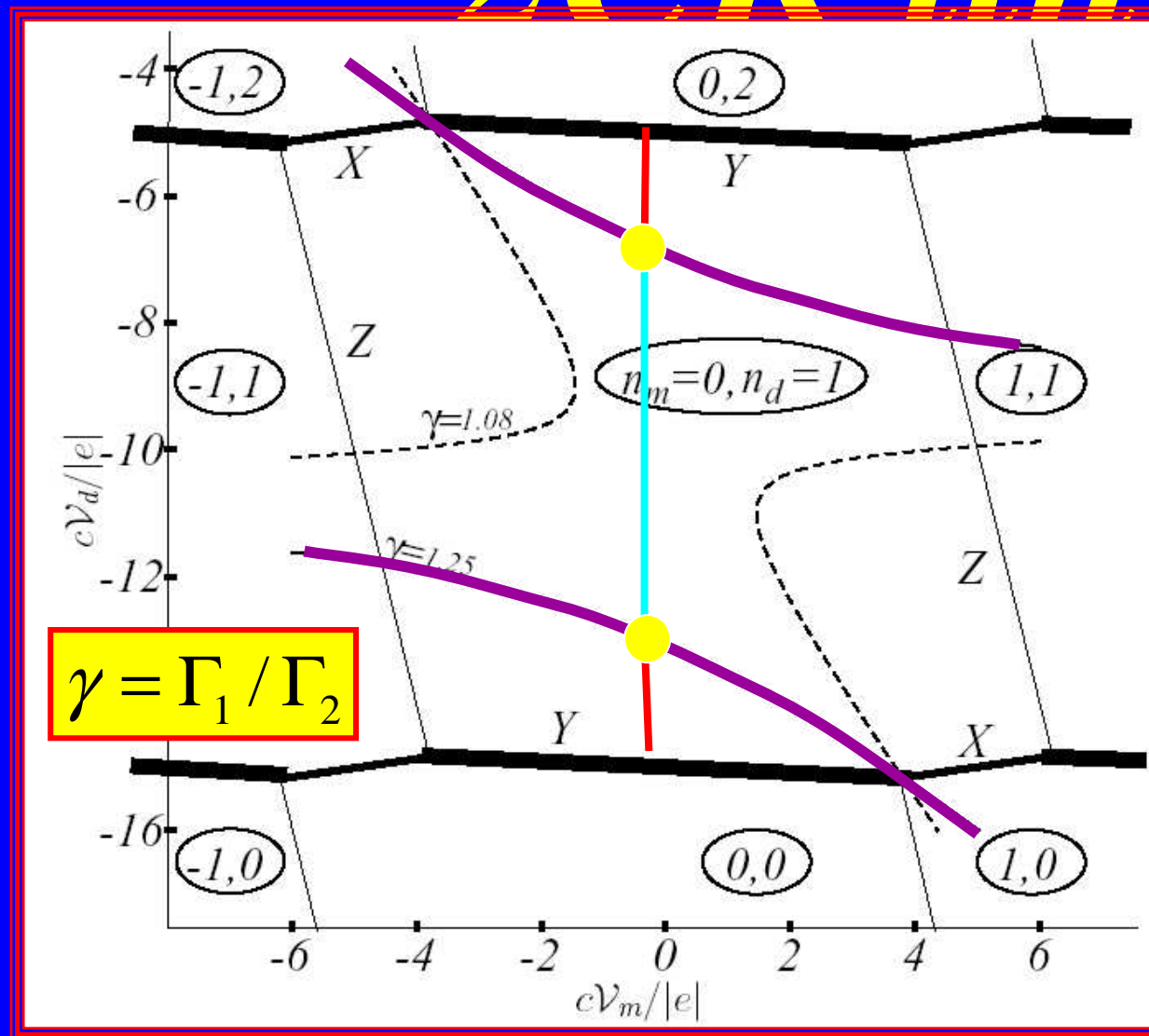
# Experimental Realization: Three leg configuration



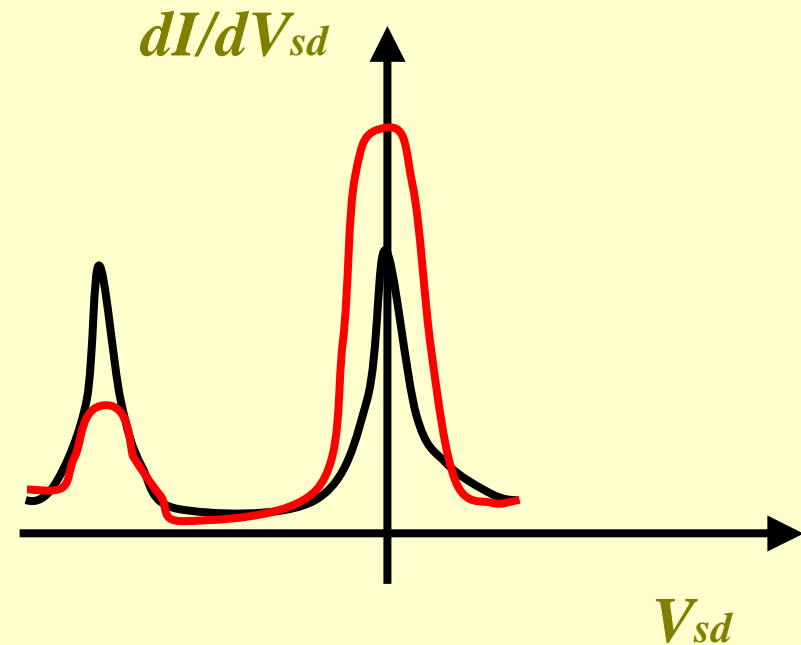
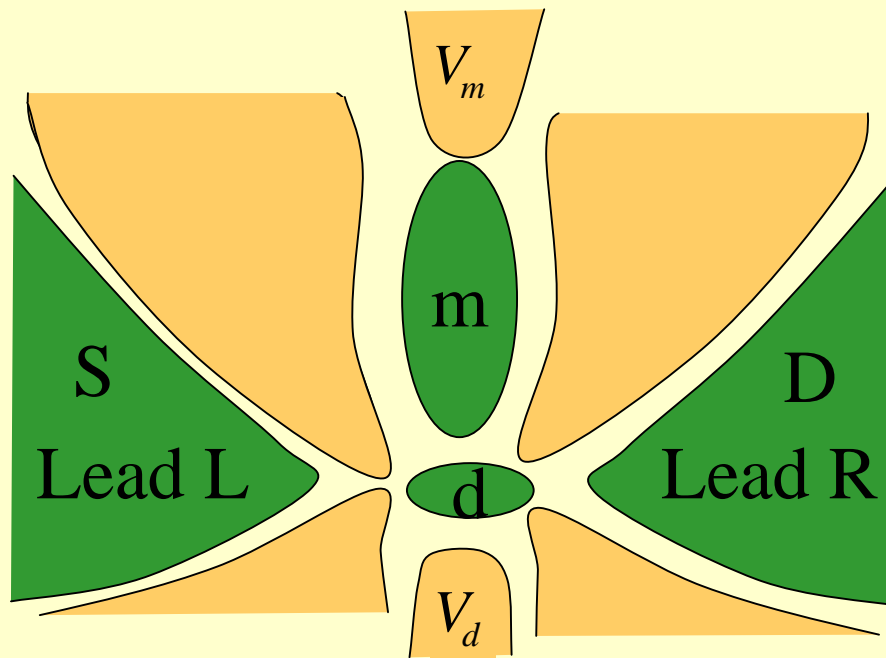
# Hexagons



# 2CK lines



# Suggestions for Experiments: Tunneling Density of states



Arcadi Shehter

# Summary

- A Realization of *two (multi) channel Kondo* in a modified Single Electron Transistor.
  - More theory (Magnetic Field and Anisotropy, dependence on initial physical parameters, Dephasing, noise, pumping, tunneling DOS) and new experiments ...
- Model: small dot + interacting leads (channels):
  - a Generalization in a new direction (each channel have different “electrochemical potential”).
  - Generic model: many other types of petals will “do the job”:
    - Luttinger liquid, Interacting disordered systems, Two 2D strongly interacting metals (Cuprates?), Environment with large impedance...